



반도체소재설계 강의자료 05

한밭대학교 신소재공학과 신기현

Machine Learning Definition

"A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P , if its performance at tasks in T , as measured by P , improves with experience E "

By Tom M. Mitchell

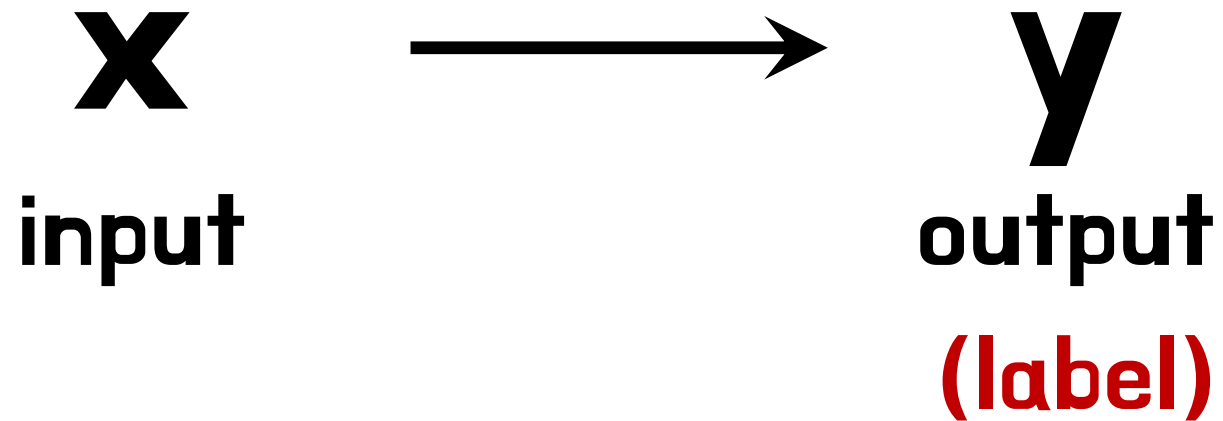


Machine Learning Algorithms

- **Supervised learning**
- **Unsupervised learning**
- **Reinforcement learning**



Supervised Learning



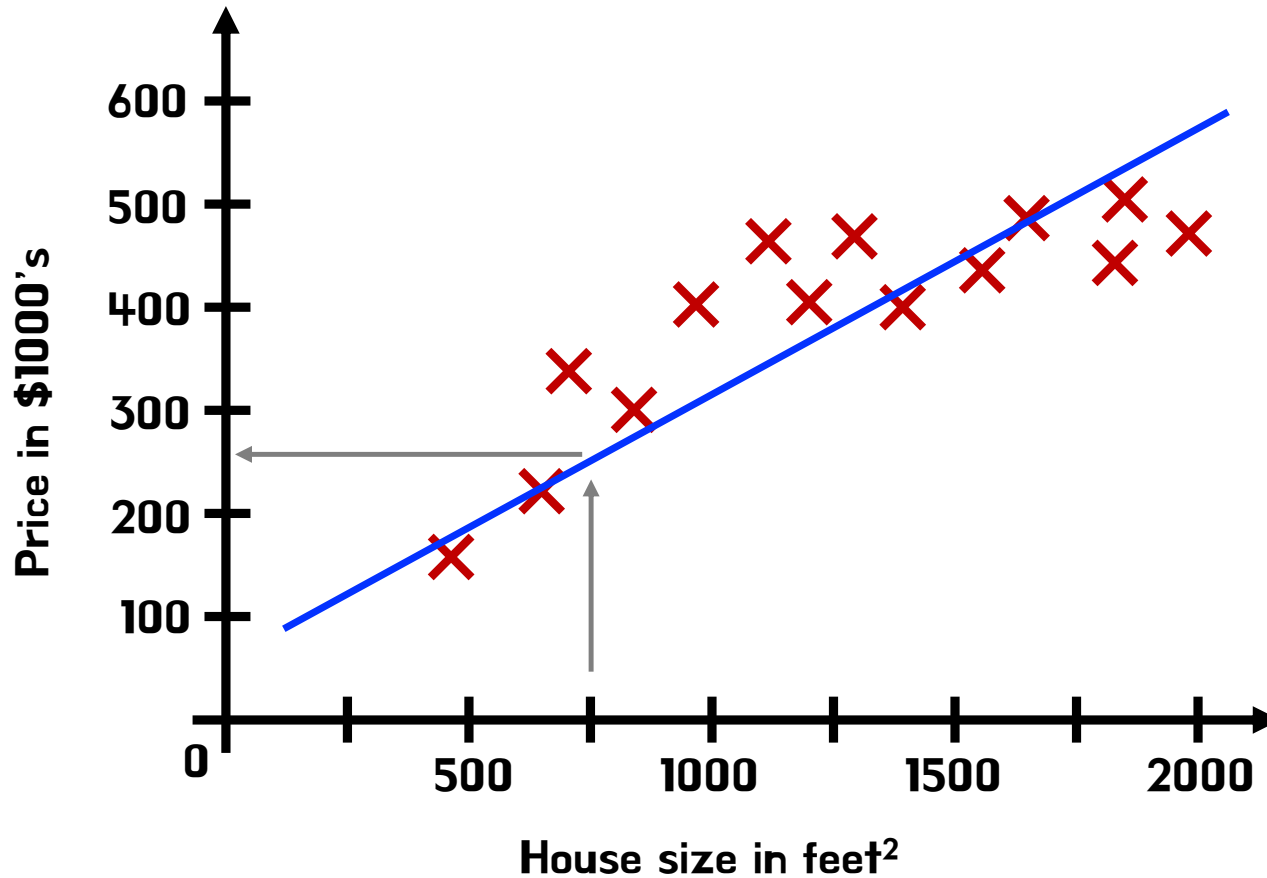
Learns from being given “**right answers**”

Supervised Learning

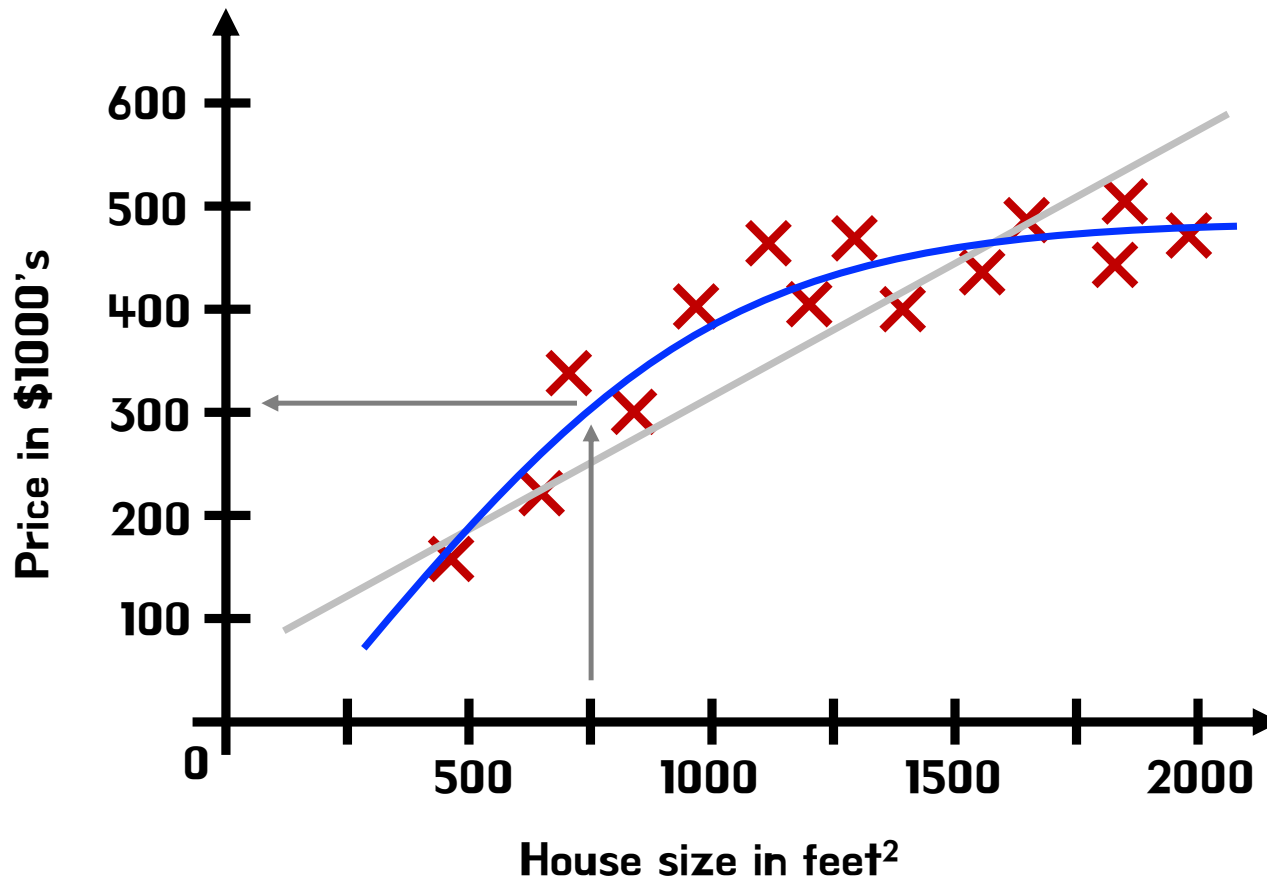
Input (x)	Output (y)	Application
email	spam? (0/1)	Spam filtering
audio	text transcripts	Speech recognition
english	spanish	Machine translation
Ad, user info.	Click ? (0/1)	Online advertising
Image, radar info.	Position of other cars	Self-driving car
Image of phone	Defect ? (0/1)	Visual inspection



Regression: Housing price prediction



Regression: Housing price prediction



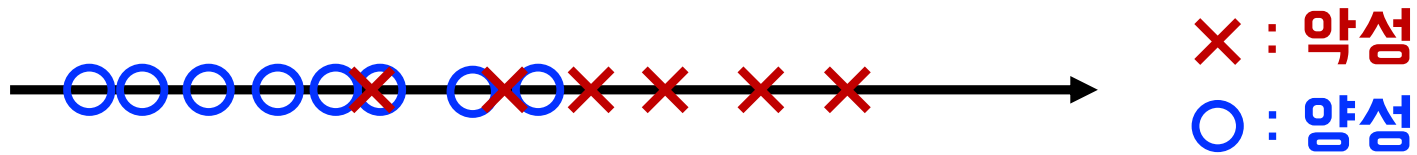
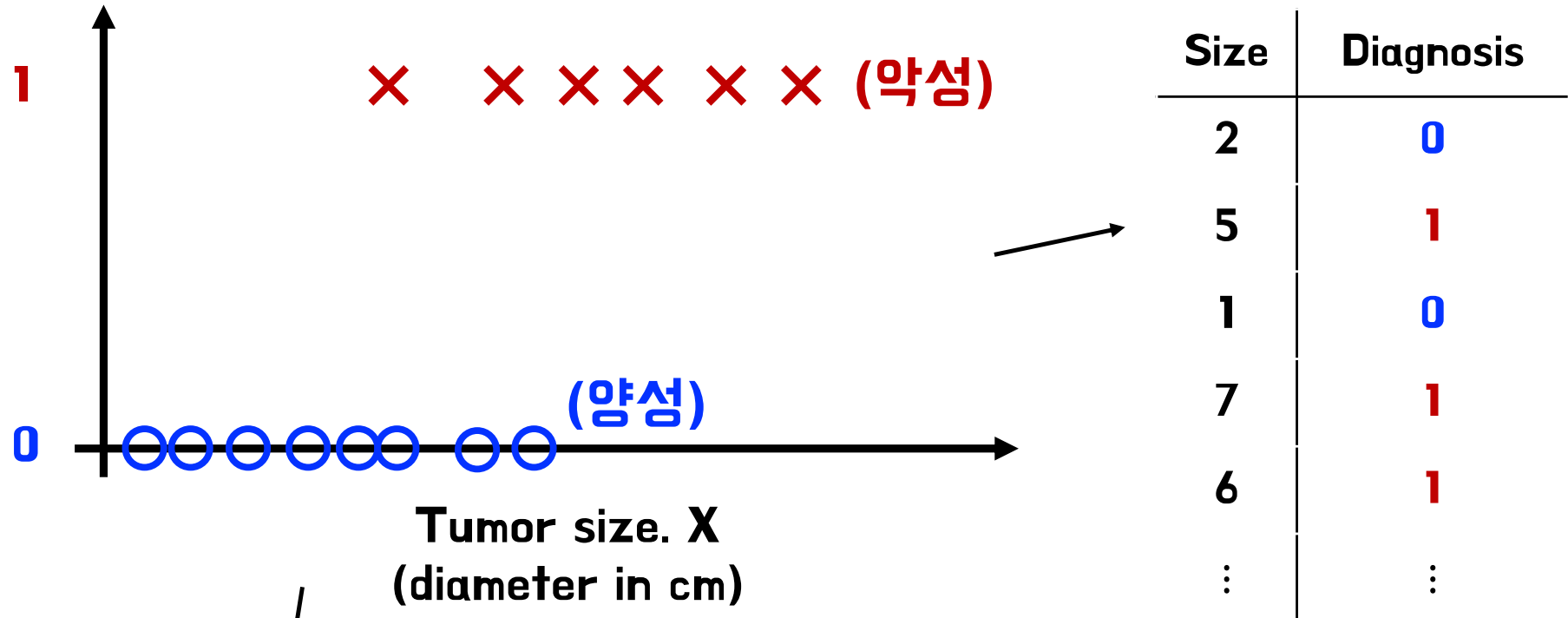
Regression

predict a number

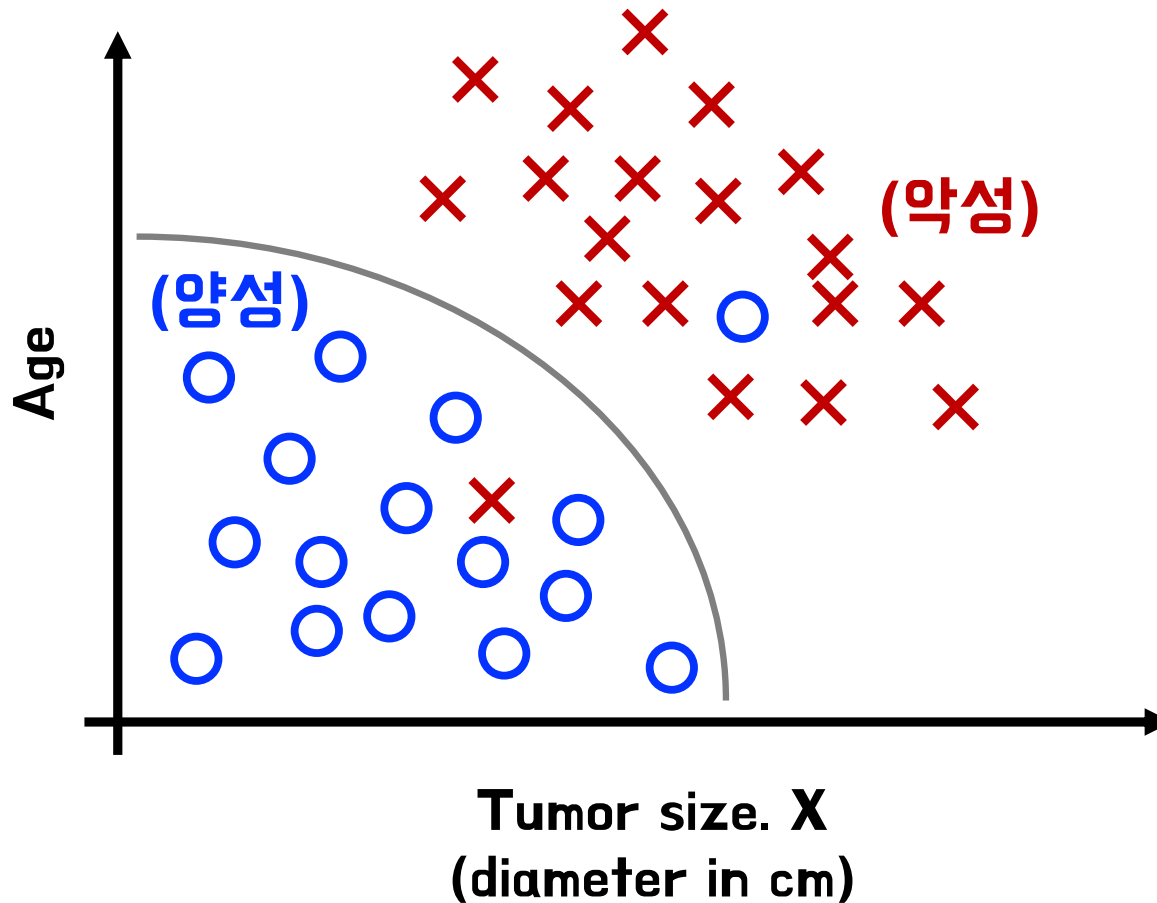
(infinitely many possible outputs)



Classification: Breast cancer detection



Two or more inputs



Many more inputs can be also available
(thickness, uniformity of size, shape)

Supervised learning

Supervised Learning

Learns from being given “**right answers**”

Regression

Predict a number

Infinitely many possible outputs

Classification

Predict categories

Small number of possible outputs

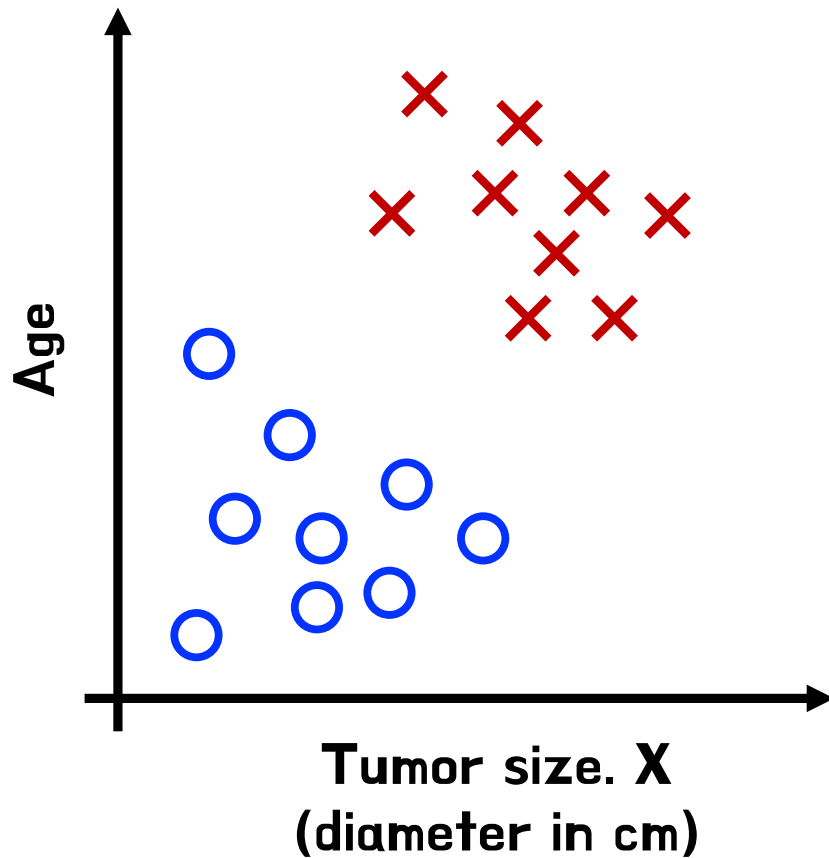


Unsupervised learning

Supervised learning

Learn from data **labeled**

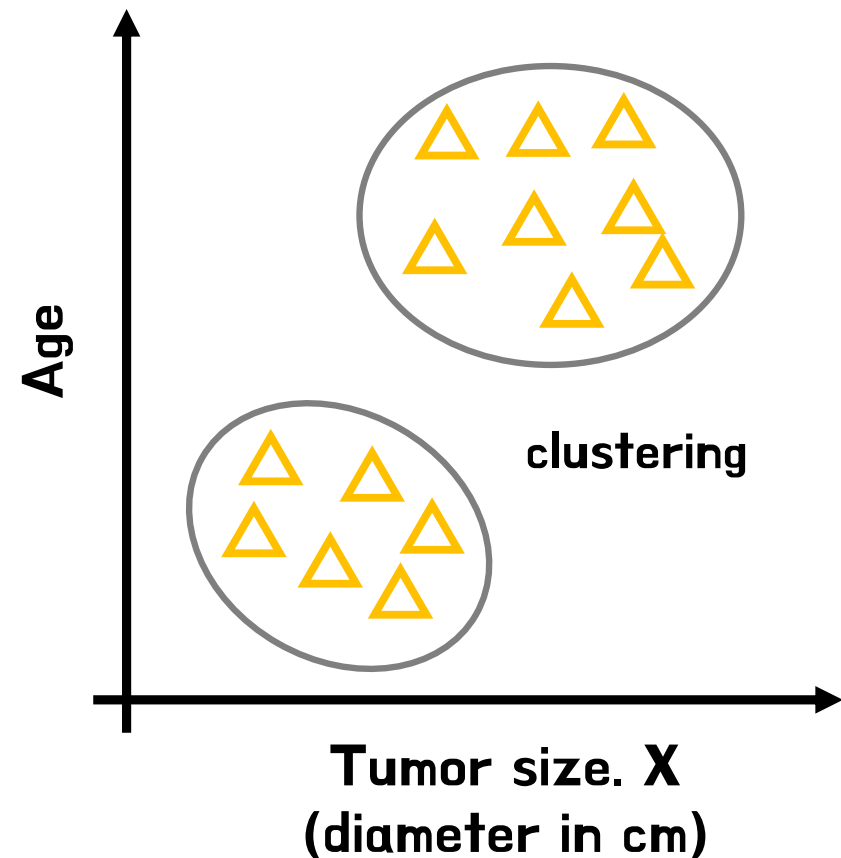
With the “**right answers**”



Unsupervised learning

Find something interesting

in **unlabeled** data



Unsupervised learning

Giant panda gives birth to rare twin cubs at Japan's oldest zoo

USA TODAY · 6 hours ago

- Giant panda gives birth to twin cubs at Japan's oldest zoo

CBS News · 7 hours ago

- Giant panda gives birth to twin cubs at Tokyo's Ueno Zoo


WHBL News · 16 hours ago

- A Joyful Surprise at Japan's Oldest Zoo: The Birth of Twin Panda

The New York Times · 1 hour ago

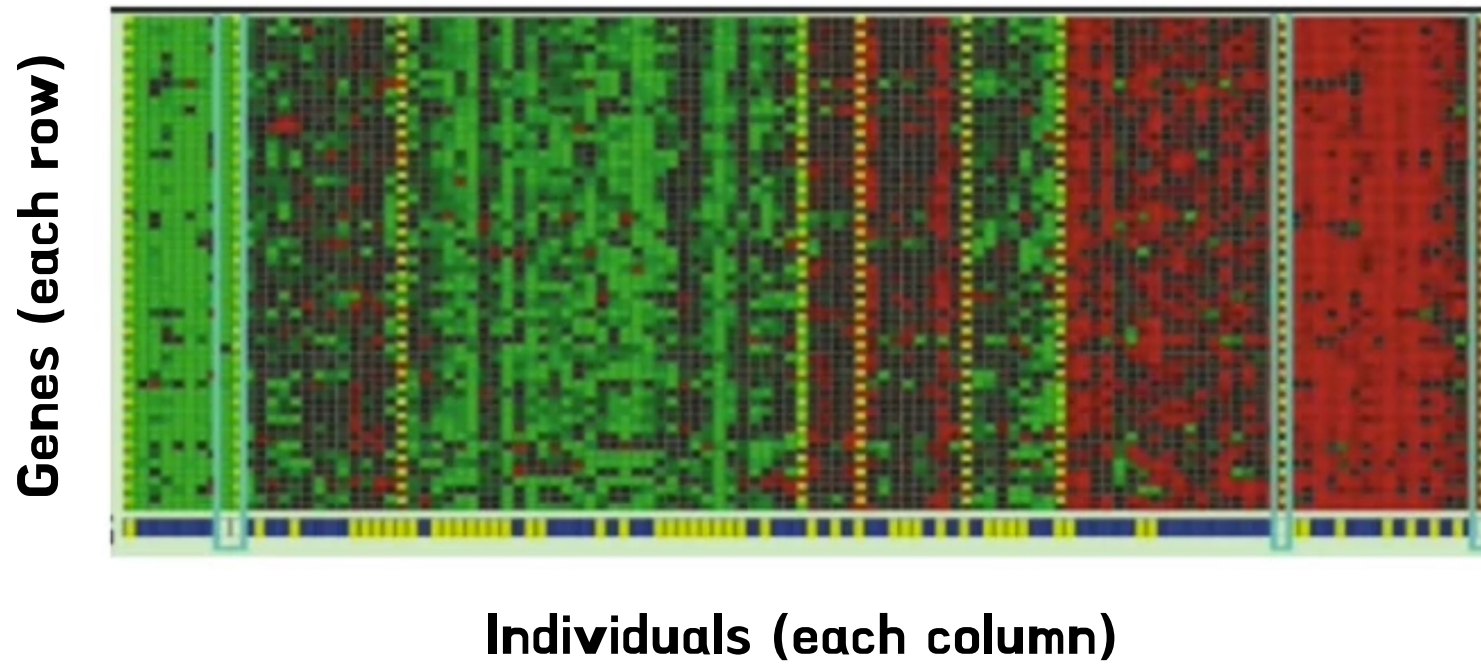
- Twin Panda Cubs Born at Tokyo's Ueno Zoo

PEOPLE · 6 hours ago

 [View Full Coverage](#)



Unsupervised learning



Unsupervised learning

Data only comes with inputs x , but not output labels y .

Algorithm has to find structure in the data.

Clustering

Group similar data points together.

Dimensionality reduction

(차원축소)

Compress data using fewer numbers.

Anomaly detection

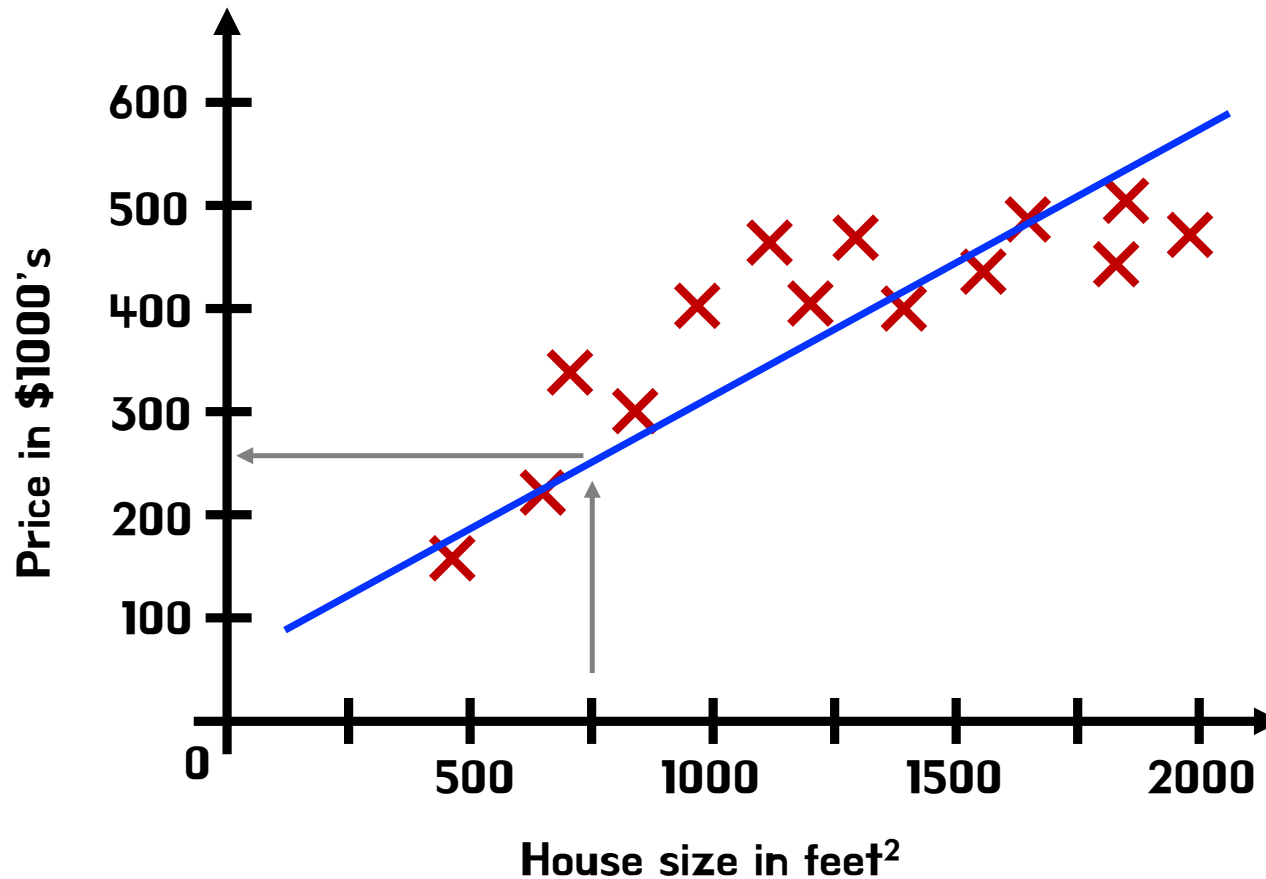
Find unusual data points.



Linear Regression (선형 회귀)



Linear regression



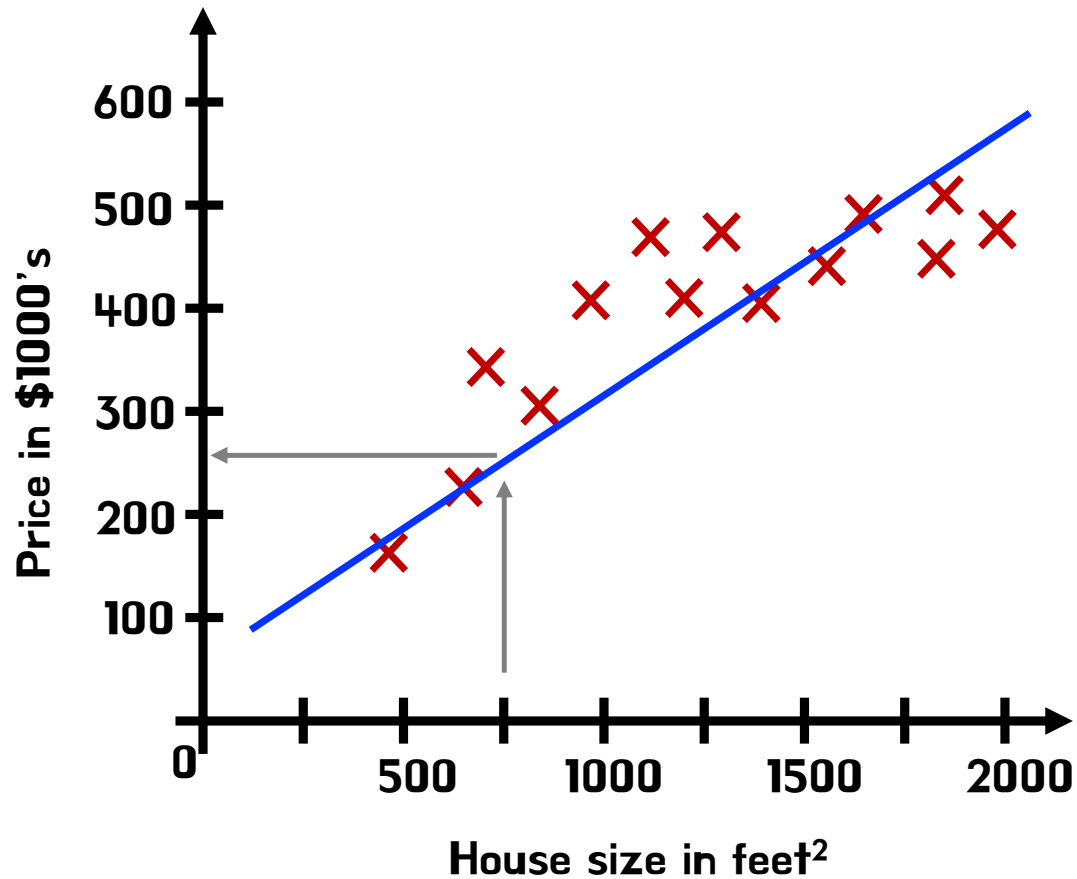
Regression model
Predicts numbers
(infinitely many possible outputs)

Supervised learning model
Data has "right answers"

Classification model
Predicts categories
(small number of possible outputs)



Linear regression



Data table

Size in feet ²	Price in \$1000's
900	310
700	320
990	400
1550	406
1700	490
⋮	⋮

Terminology

Training set : Data used to train the model

	x Size in feet ²	y Price in \$1000's
(1)	900	310
(2)	700	320
(3)	990	400
(4)	1550	406
(5)	1700	490
⋮	⋮	⋮

Test set : Data used to test the model

	Size in feet ²	Price in \$1000's
(a)	980	310
(b)	1300	390
(c)	2000	500

Notation:

x = “input” variable
feature

y = “output” variable
“target” variable

m = number of training examples

(x, y) = single training example

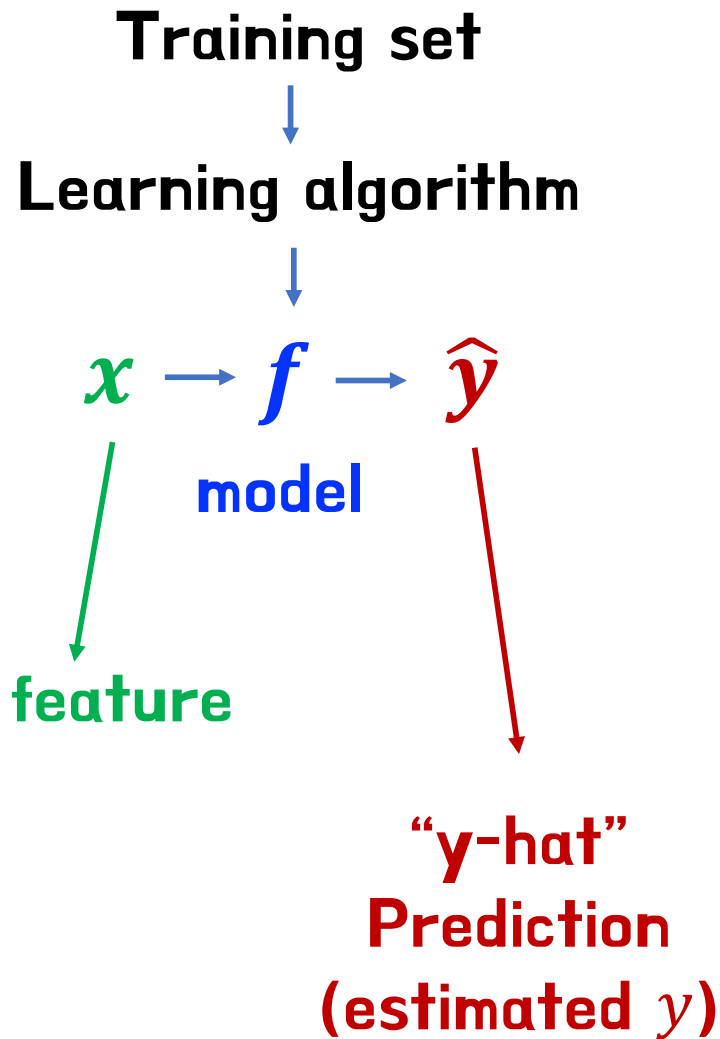
(x⁽ⁱ⁾, y⁽ⁱ⁾) = ith training example

x = 900, y = 400

(x, y) = (900, 400)

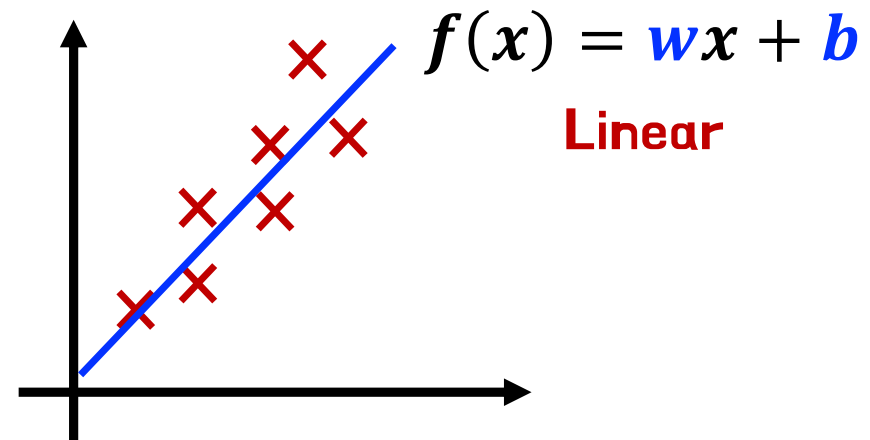


Terminology



How to represent f ?

$$f_{w,b}(x) = f(x) = wx + b$$



Linear regression with one variable.
Univariate linear regression.

Parameters (Hyper parameters)

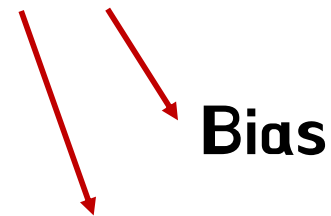
Training set

(feature) (targets)

Size in feet ²	Price in \$1000's
900	310
700	320
990	400
1550	406
1700	490
⋮	⋮

$$f(x) = wx + b$$

w, b : parameters

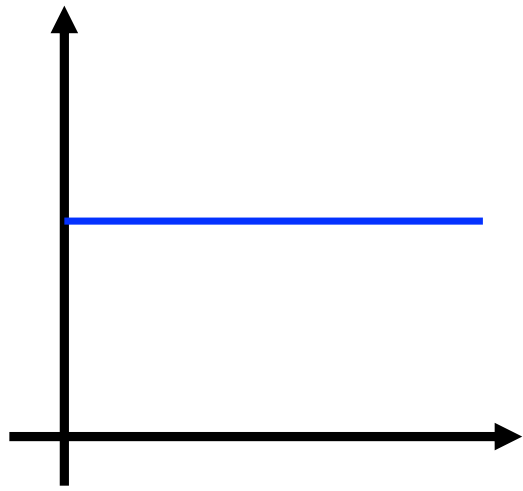
 Bias

Weights

What do w, b do ?

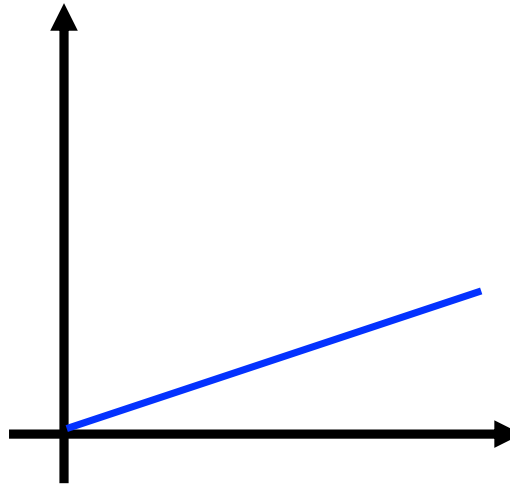
Cost function

$$f(x) = wx + b$$



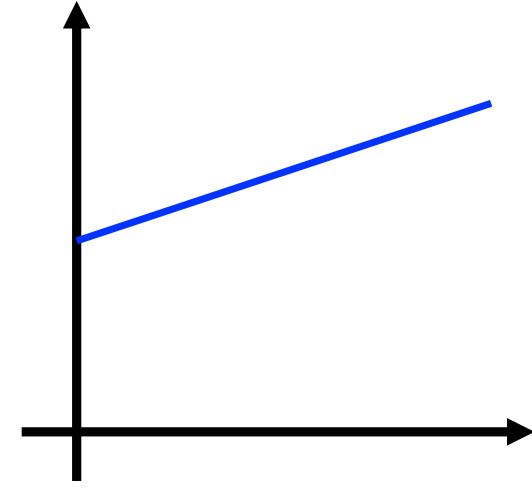
$$w = 0$$

$$b = 1.5$$



$$w = 0.5$$

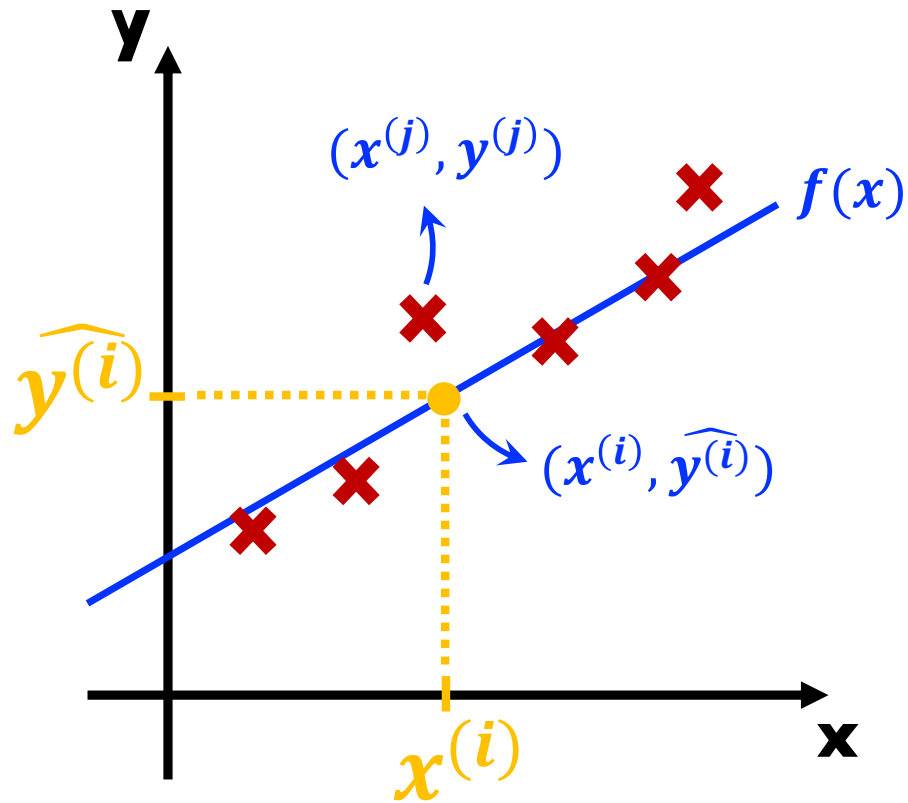
$$b = 0$$



$$w = 0.5$$

$$b = 1$$

Cost function



$$\widehat{y}^{(i)} = f(x^{(i)}) = wx^{(i)} + b$$

Cost function:
Squared error cost function

$$J(w, b) = \frac{1}{2m} \sum_{i=1}^m (\widehat{y}^{(i)} - y^{(i)})^2$$

error

Number of training examples

$$J(w, b) = \frac{1}{2m} \sum_{i=1}^m (f(x^{(i)}) - y^{(i)})^2$$

$$J(w, b) = \frac{1}{2m} \sum_{i=1}^m (wx^{(i)} + b - y^{(i)})^2$$



Cost function

Model:

$$f(x) = wx + b$$

Parameters:

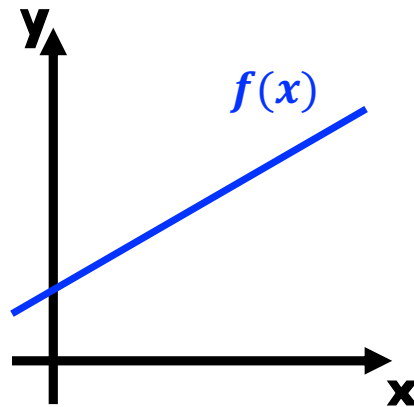
$$w, b$$

Cost function:

$$J(w, b) = \frac{1}{2m} \sum_{i=1}^m (f(x^{(i)}) - y^{(i)})^2$$

Goal:

$$\begin{aligned} &\text{minimize } J(w, b) \\ &w, b \end{aligned}$$



Simplified Model:

$$f(x) = wx$$

Parameters:

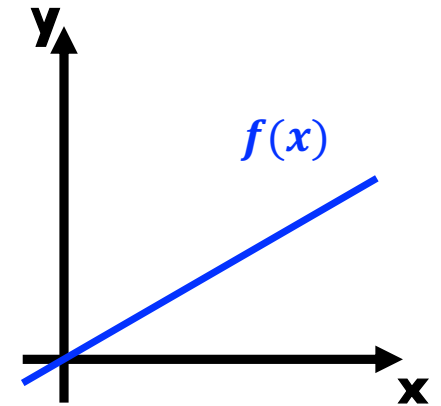
$$w$$

Cost function:

$$J(w) = \frac{1}{2m} \sum_{i=1}^m (f(x^{(i)}) - y^{(i)})^2$$

Goal:

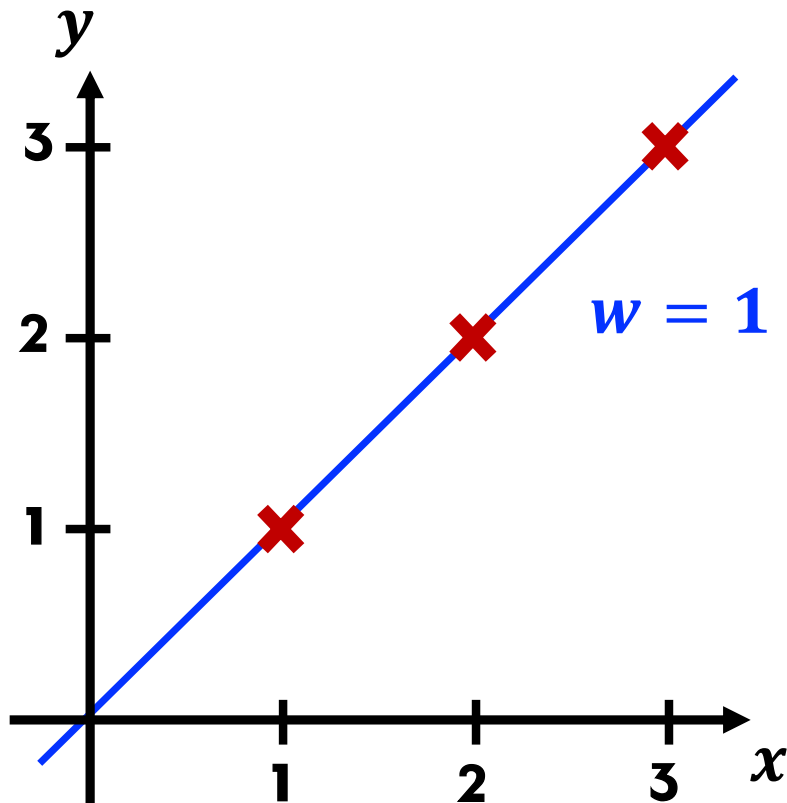
$$\begin{aligned} &\text{minimize } J(w) \\ &w \end{aligned}$$



Cost function

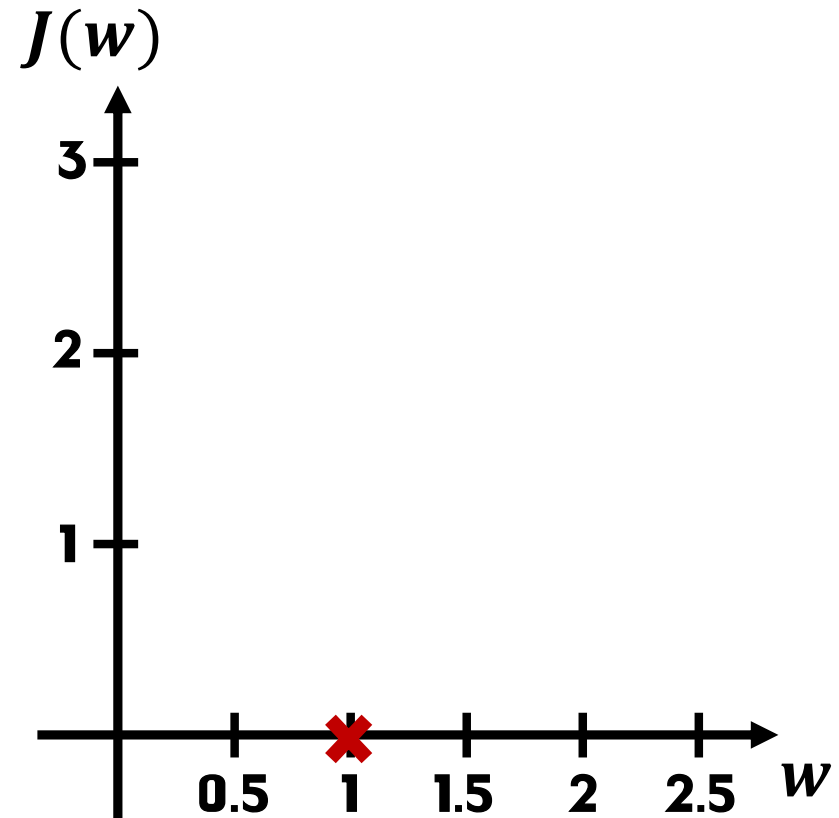
$$f_w(x)$$

For fixed w , function of x



$$J(w)$$

Function of w



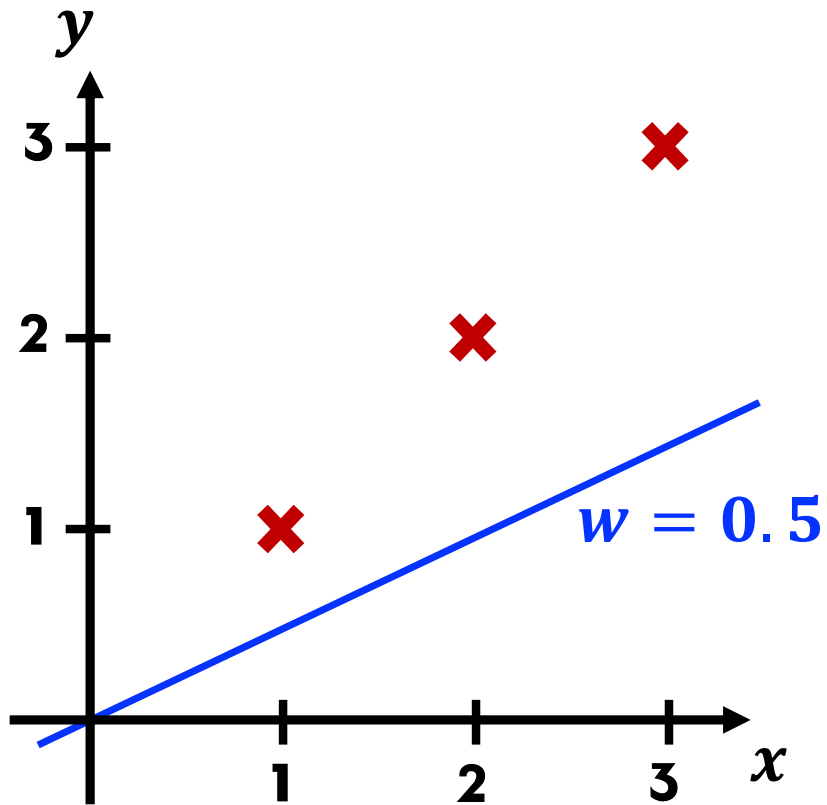
$$J(w) = \frac{1}{2m} \sum_{i=1}^m (f(x^{(i)}) - y^{(i)})^2 = \frac{1}{2m} \sum_{i=1}^m (wx^{(i)} - y^{(i)})^2 = \frac{1}{2m} (0^2 + 0^2 + 0^2) = 0$$



Cost function

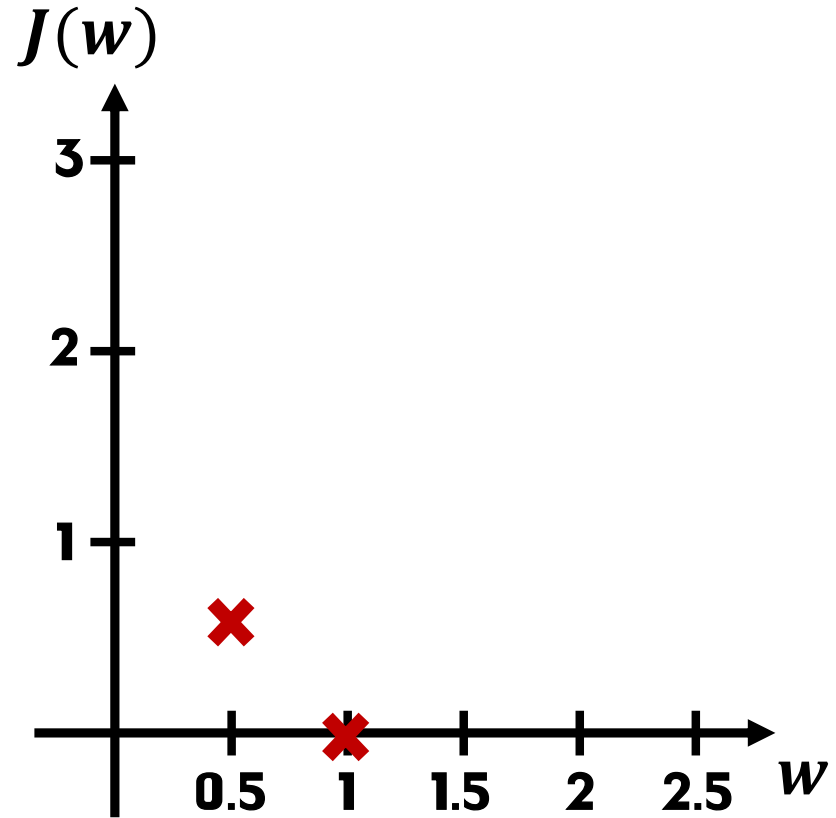
$$f_w(x)$$

For fixed w , function of x



$$J(w)$$

Function of w



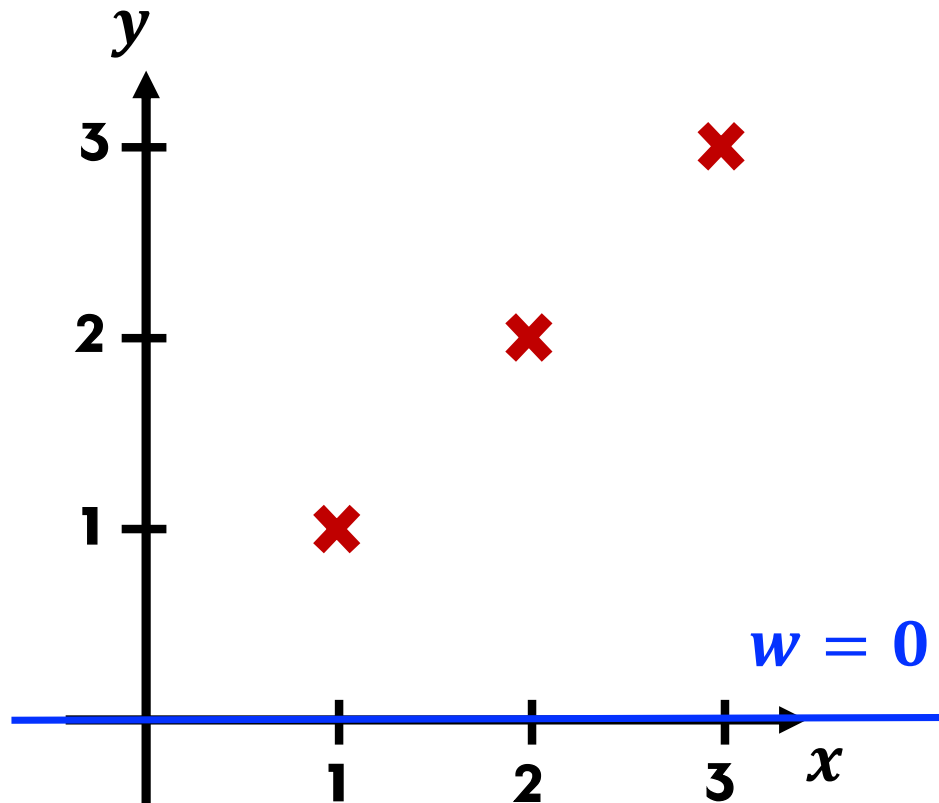
$$J(w) = \frac{1}{2m} \left((0.5 - 1)^2 + (1 - 2)^2 + (1.5 - 3)^2 \right) = \frac{3.5}{6} = 0.58$$



Cost function

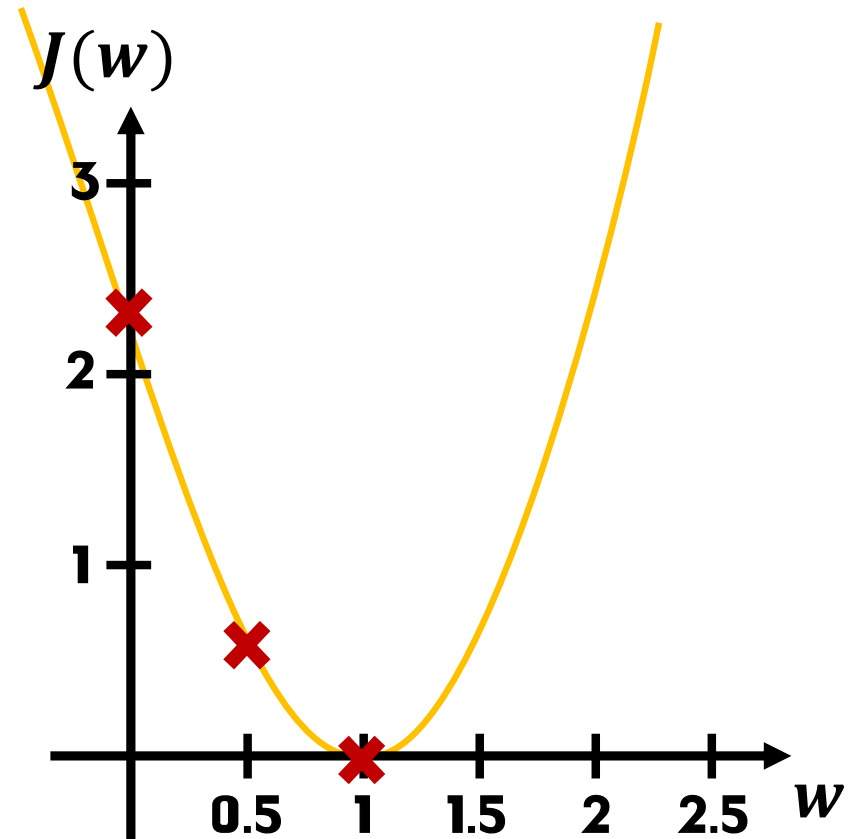
$$f_w(x)$$

For fixed w , function of x



$$J(w)$$

Function of w

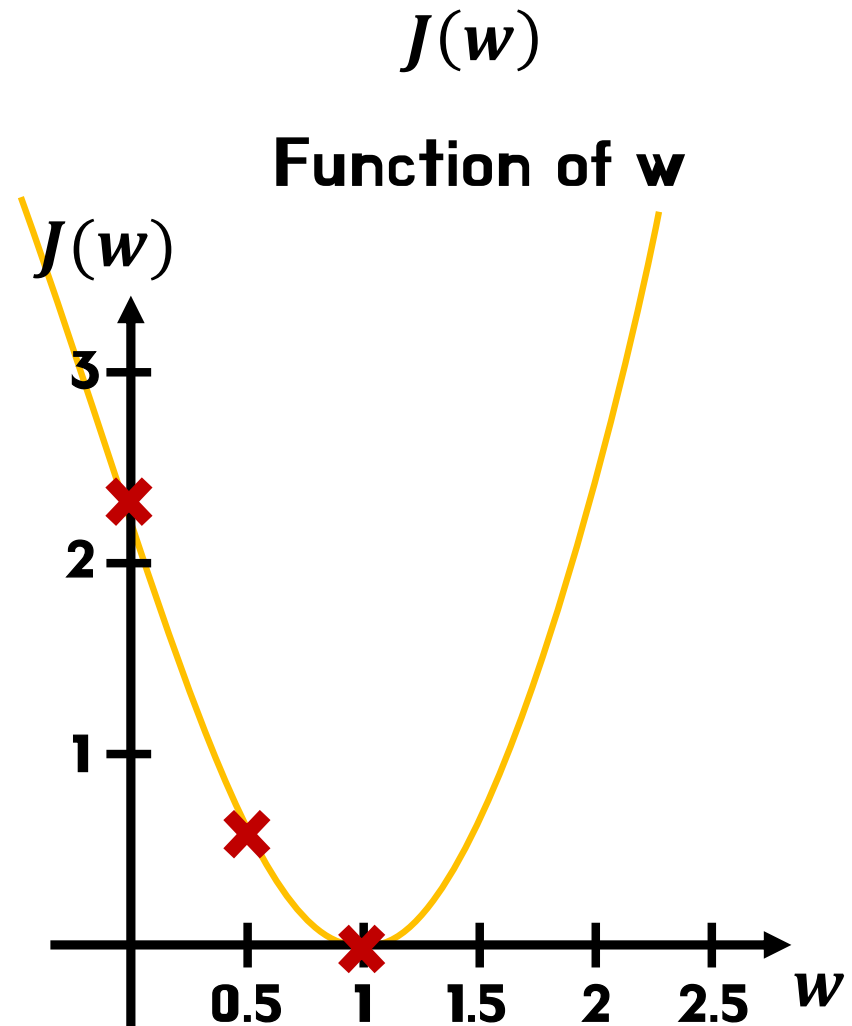


$$J(w) = \frac{1}{2m} \left((1)^2 + (2)^2 + (3)^2 \right) = \frac{14}{6} = 2.3$$



Cost function

Goal of linear regression:
minimize $J(w)$



Choose w to minimize $J(w)$

Logistic Regression **: classification** **(로지스틱 회귀)**

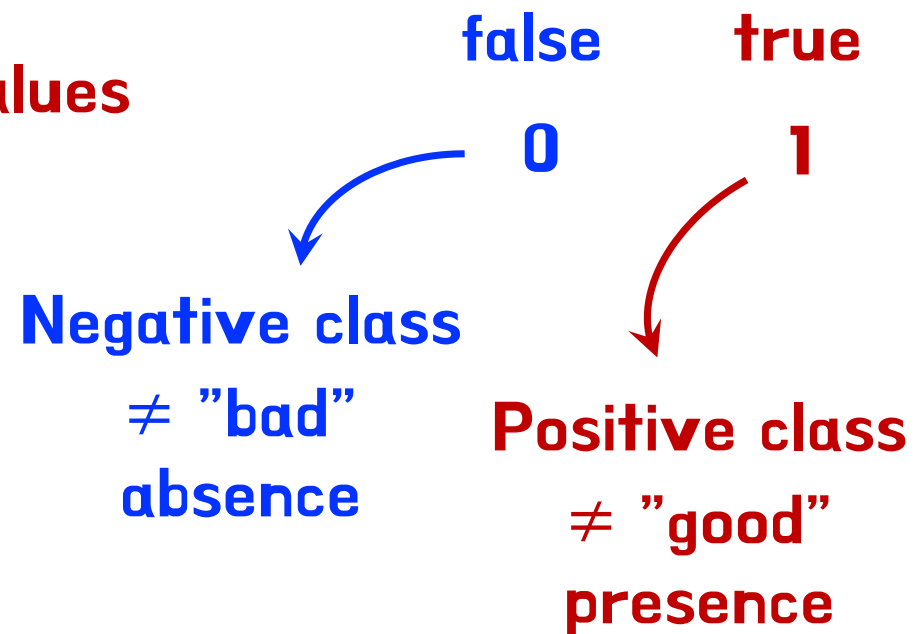


Classification

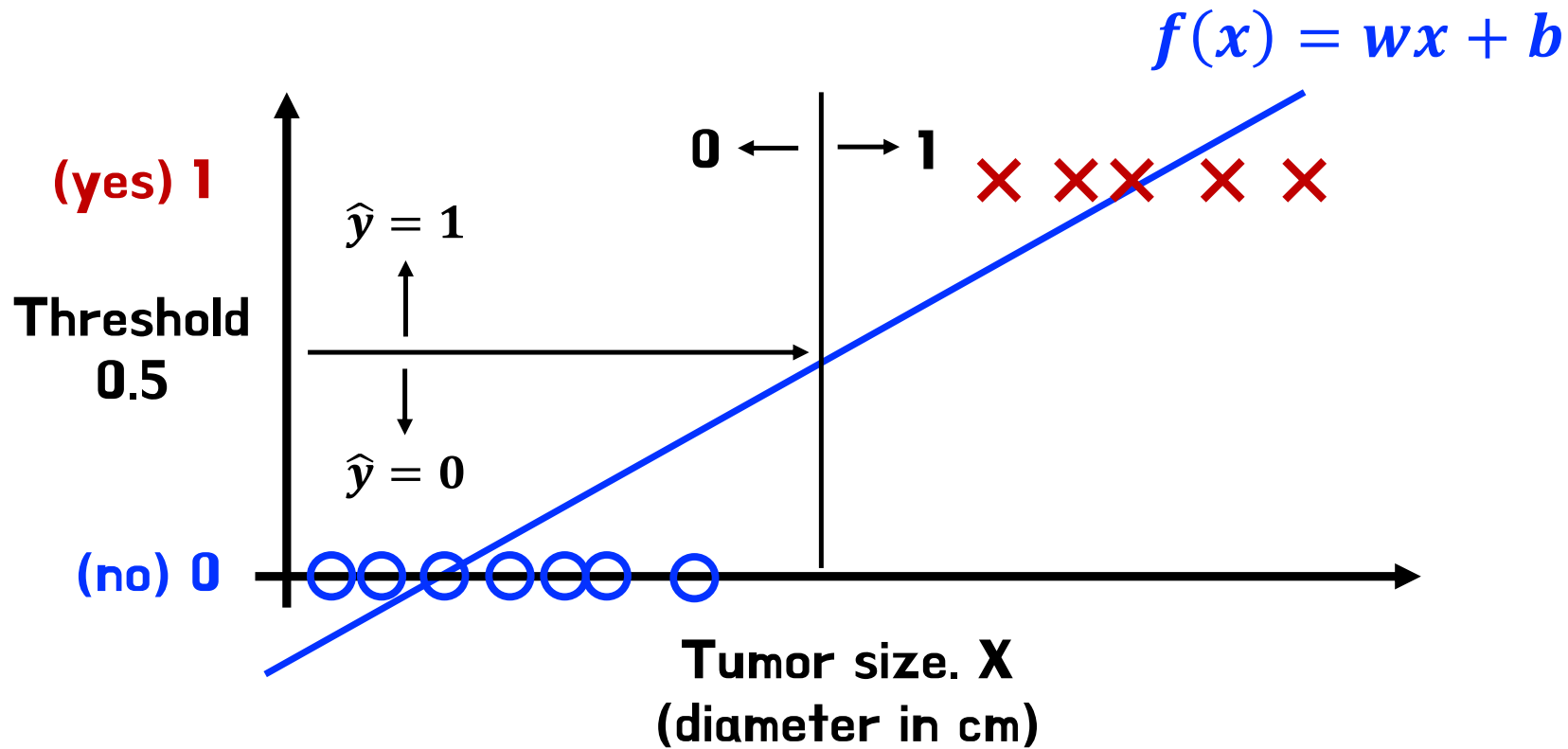
Question	Answer “y”	
Is this email spam ?	no	yes
Is the transaction fraudulent?	no	yes
Is the tumor malignant?	no	yes

y can only be **one of two values**

“binary **classification**”
= **category**



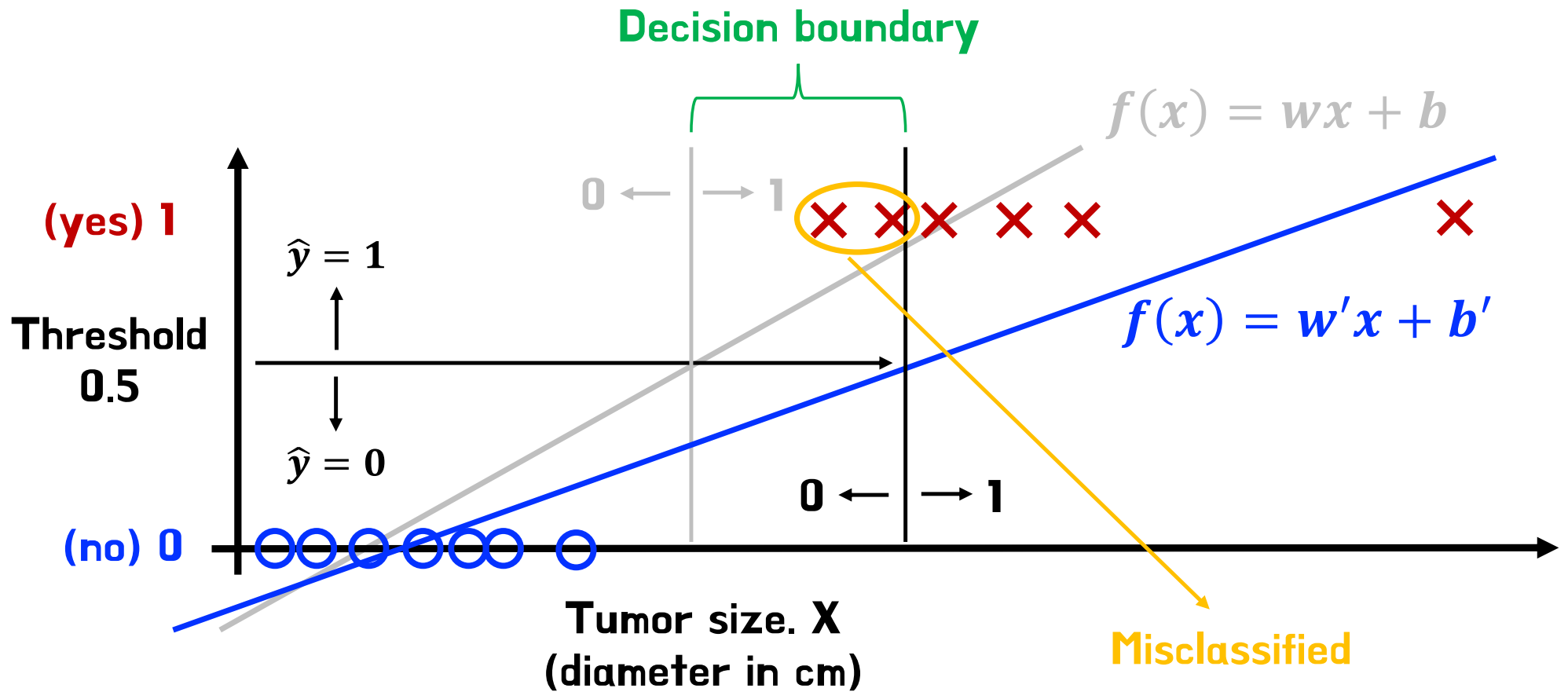
Linear regression



$$\text{If } f(x) < 0.5 \rightarrow \hat{y} = 0$$

$$\text{If } f(x) \geq 0.5 \rightarrow \hat{y} = 1$$

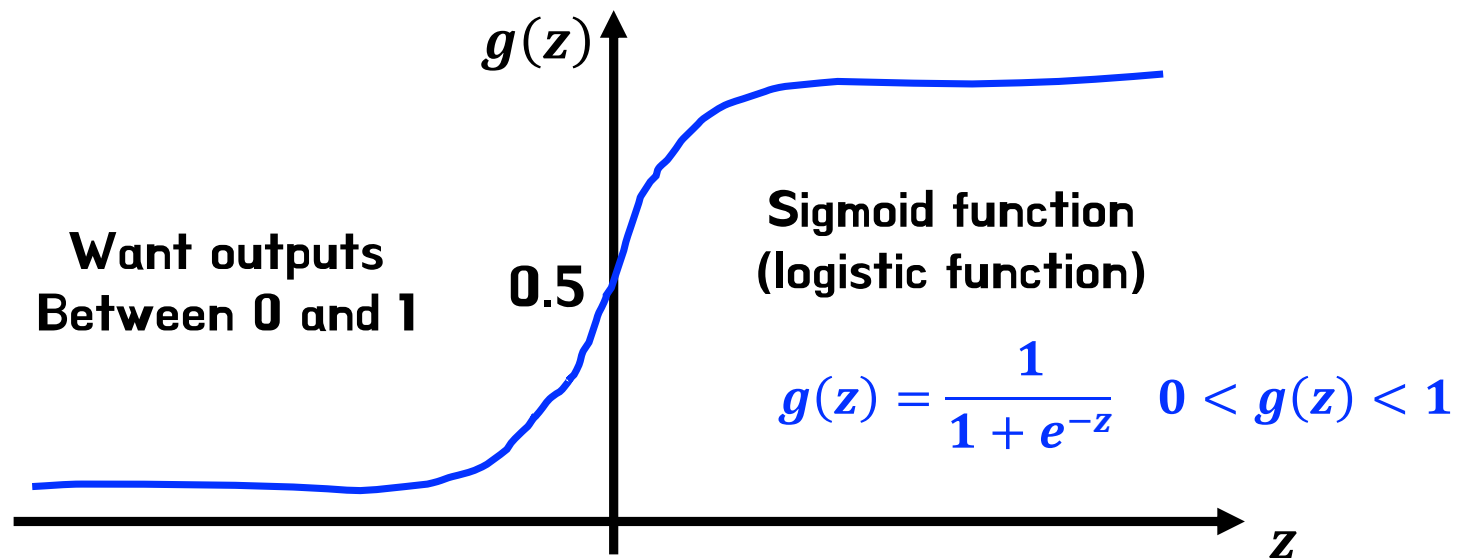
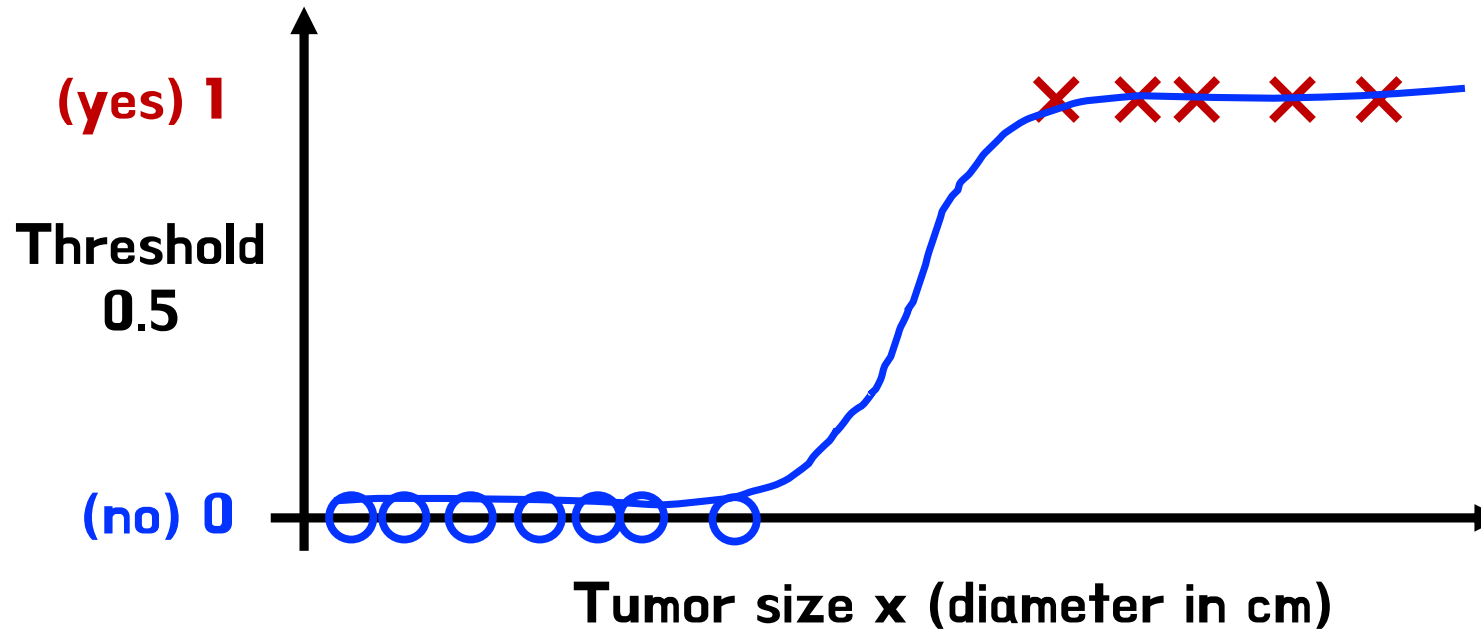
Linear regression



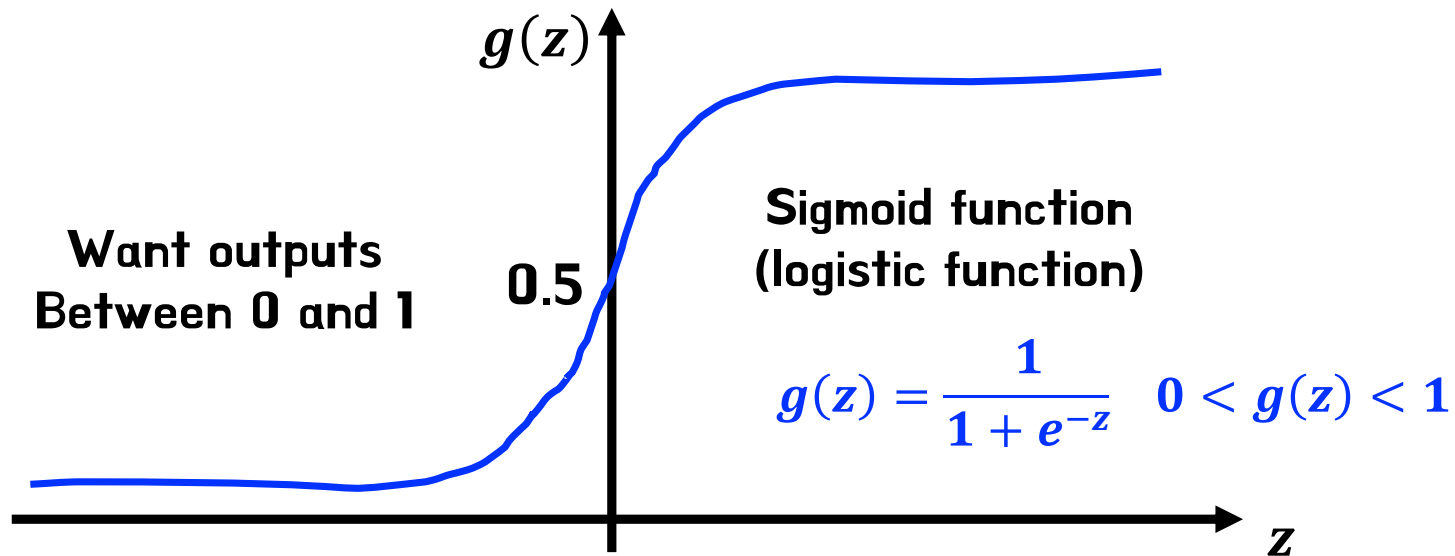
$$\text{If } f(x) < 0.5 \rightarrow \hat{y} = 0$$

$$\text{If } f(x) \geq 0.5 \rightarrow \hat{y} = 1$$

Logistic regression



Logistic regression



$f_{w,b}(x) = wx + b$
in linear regression

$$z = wx + b$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$f_{w,b}(x) = g(\underset{= z}{wx + b}) = \frac{1}{1 + e^{-(wx+b)}}$$

“Logistic regression”

Logistic regression

$$f_{w,b}(x) = \frac{1}{1 + e^{-(wx+b)}}$$

“probability” that class is **1**

Example:

x is “tumor size”

y is **0** (양성)

or **1** (악성)

$$f_{w,b}(x) = 0.7$$

70% chance that y is **1**

$$f_{w,b}(x) = P(y = 1 | x; w, b)$$

Probability that y is 1,
given input x , parameters w, b

$$P(y = 0) + P(y = 1) = 1 |$$

Logistic regression

$$f_{w,b}(x) = g(\mathbf{w}x + \mathbf{b}) = \frac{1}{1 + e^{-(\mathbf{w}x + \mathbf{b})}}$$
$$= P(y = 1 \mid x; w, b)$$

Is $f_{w,b}(x) \geq 0.5$? **Yes: $\hat{y} = 1$** **No: $\hat{y} = 0$**

When is $f_{w,b}(x) \geq 0.5$?

$$g(z) \geq 0.5$$

$$z \geq 0$$

$$\mathbf{w}x + \mathbf{b} \geq 0$$

$$\hat{y} = 1$$

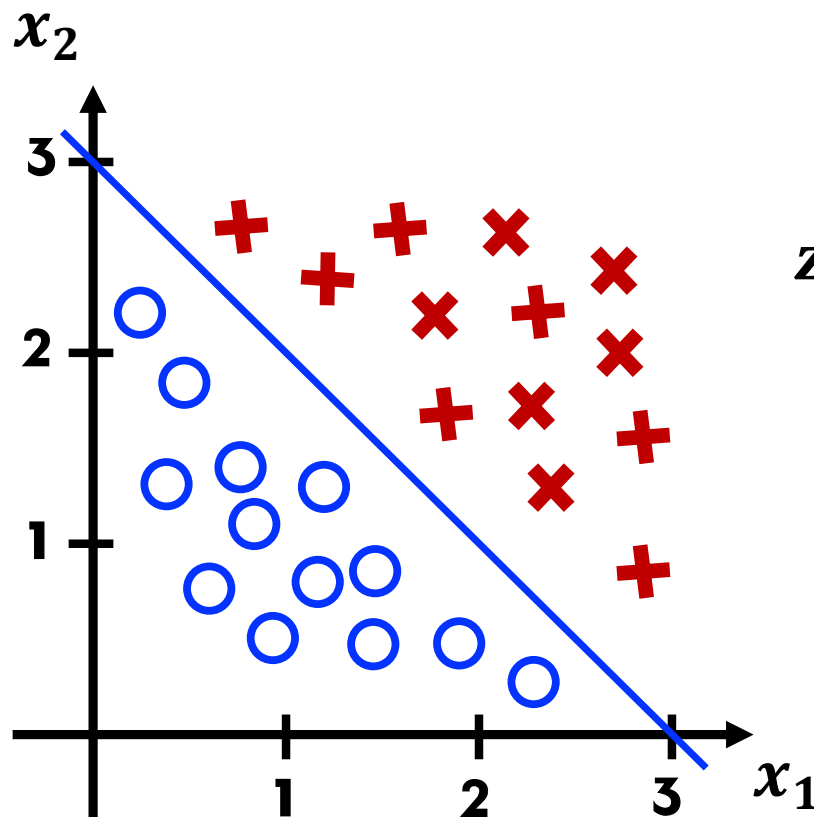
$$\mathbf{w}x + \mathbf{b} < 0$$

$$\hat{y} = 0$$



Decision boundary

$$f_{w,b}(x) = g(z) = g(\underbrace{w_1}_{1}x_1 + \underbrace{w_2}_{1}x_2 + \underbrace{b}_{-3})$$

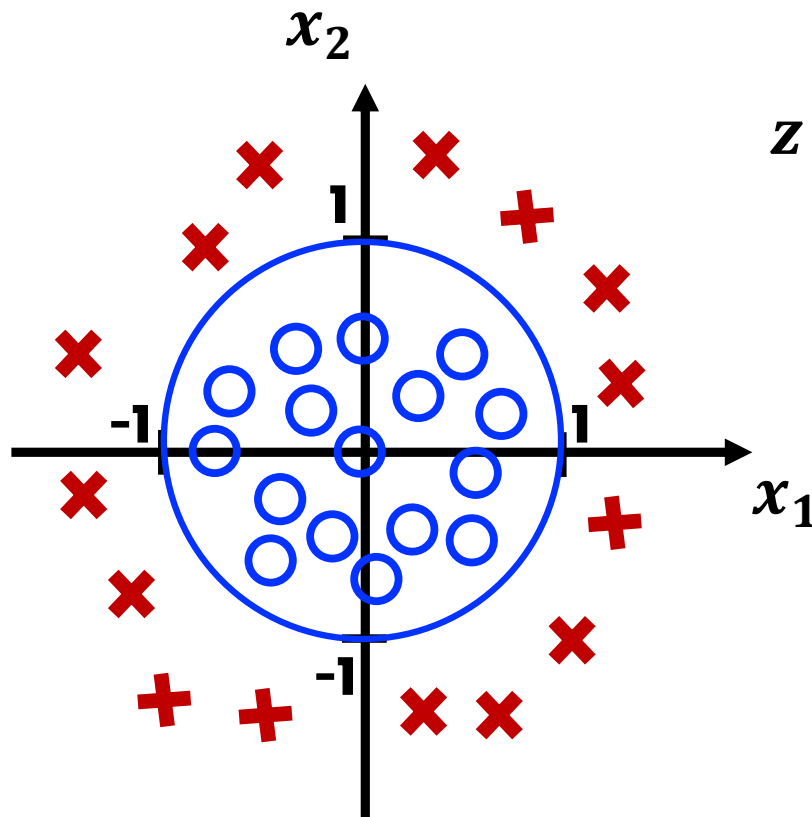


$$z = wx + b = 0$$
$$= x_1 + x_2 - 3 = 0$$

$$x_1 + x_2 = 3$$

Non-linear decision boundaries

$$f_{w,b}(x) = g(z) = g(\underbrace{w_1}_{1}x_1^2 + \underbrace{w_2}_{1}x_2^2 + \underbrace{b}_{-1})$$



$$z = x_1^2 + x_2^2 - 1 = 0$$

$$x_1^2 + x_2^2 = 1$$

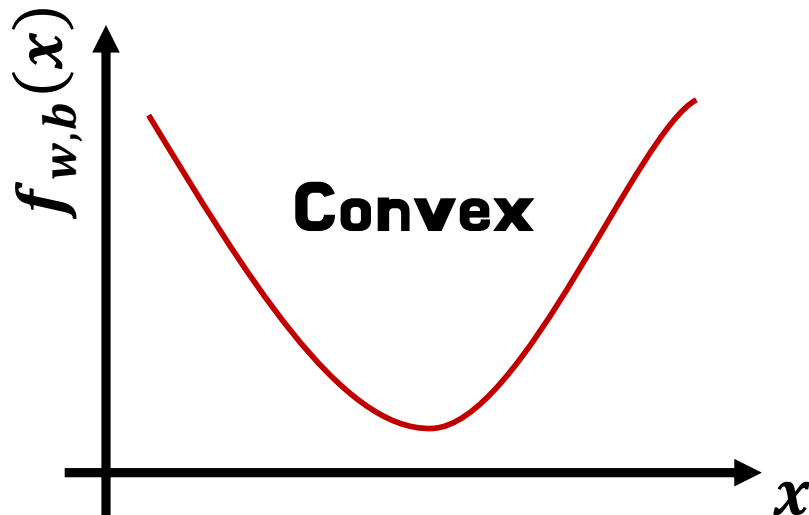
Squared error cost

$$J(w, b) = \frac{1}{m} \sum_{i=1}^m \frac{1}{2} (f(x^{(i)}) - y^{(i)})^2$$

$= L(f(x^{(i)}), y^{(i)})$ **Loss**

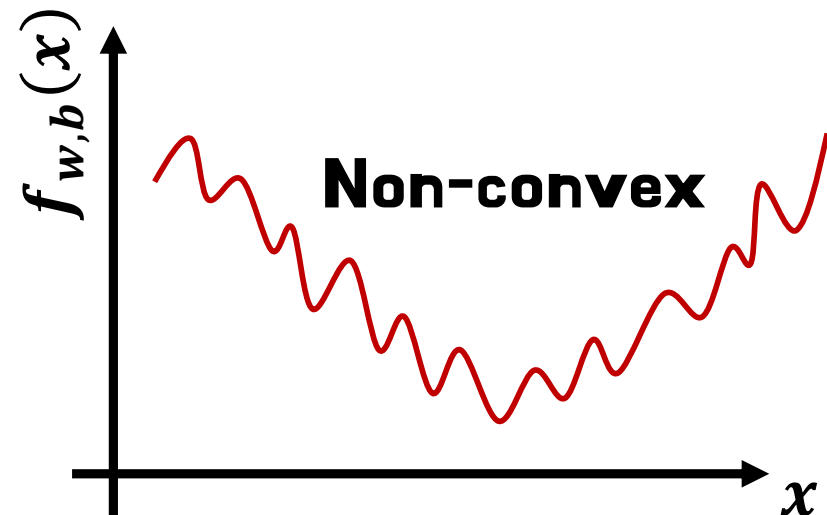
Linear regression

$$f_{w,b}(x) = wx + b$$



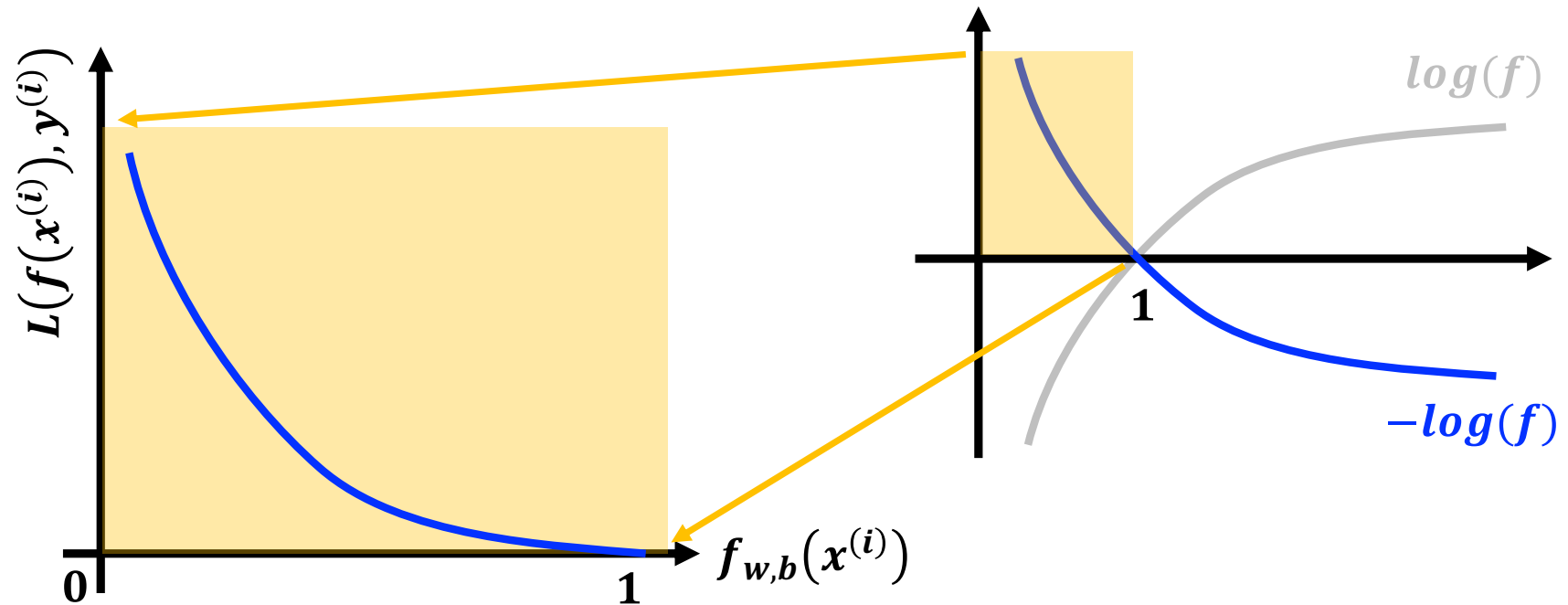
Logistic regression

$$f_{w,b}(x) = \frac{1}{1 + e^{-(wx+b)}}$$



Loss function

$$L(f(x^{(i)}), y^{(i)}) = \begin{cases} -\log(f_{w,b}(x^{(i)})) & \text{if } y^{(i)} = 1 \\ -\log(1 - f_{w,b}(x^{(i)})) & \text{if } y^{(i)} = 0 \end{cases}$$

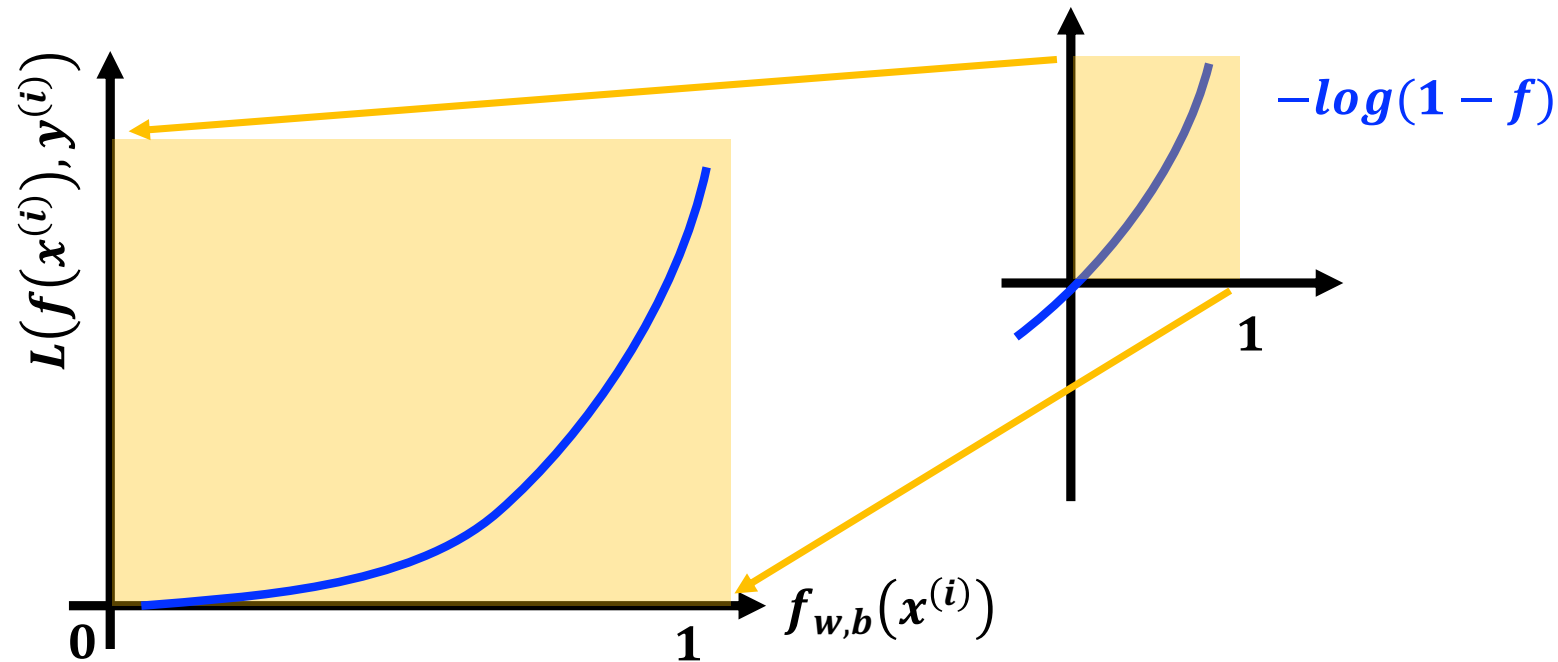


As $f_{w,b}(x^{(i)}) \rightarrow 1$ then loss $\rightarrow 0$

As $f_{w,b}(x^{(i)}) \rightarrow 0$ then loss \rightarrow infinite

Loss function

$$L(f(x^{(i)}), y^{(i)}) = \begin{cases} -\log(f_{w,b}(x^{(i)})) & \text{if } y^{(i)} = 1 \\ -\log(1 - f_{w,b}(x^{(i)})) & \text{if } y^{(i)} = 0 \end{cases}$$



As $f_{w,b}(x^{(i)}) \rightarrow 1$ then loss \rightarrow infinite

As $f_{w,b}(x^{(i)}) \rightarrow 0$ then loss $\rightarrow 0$