



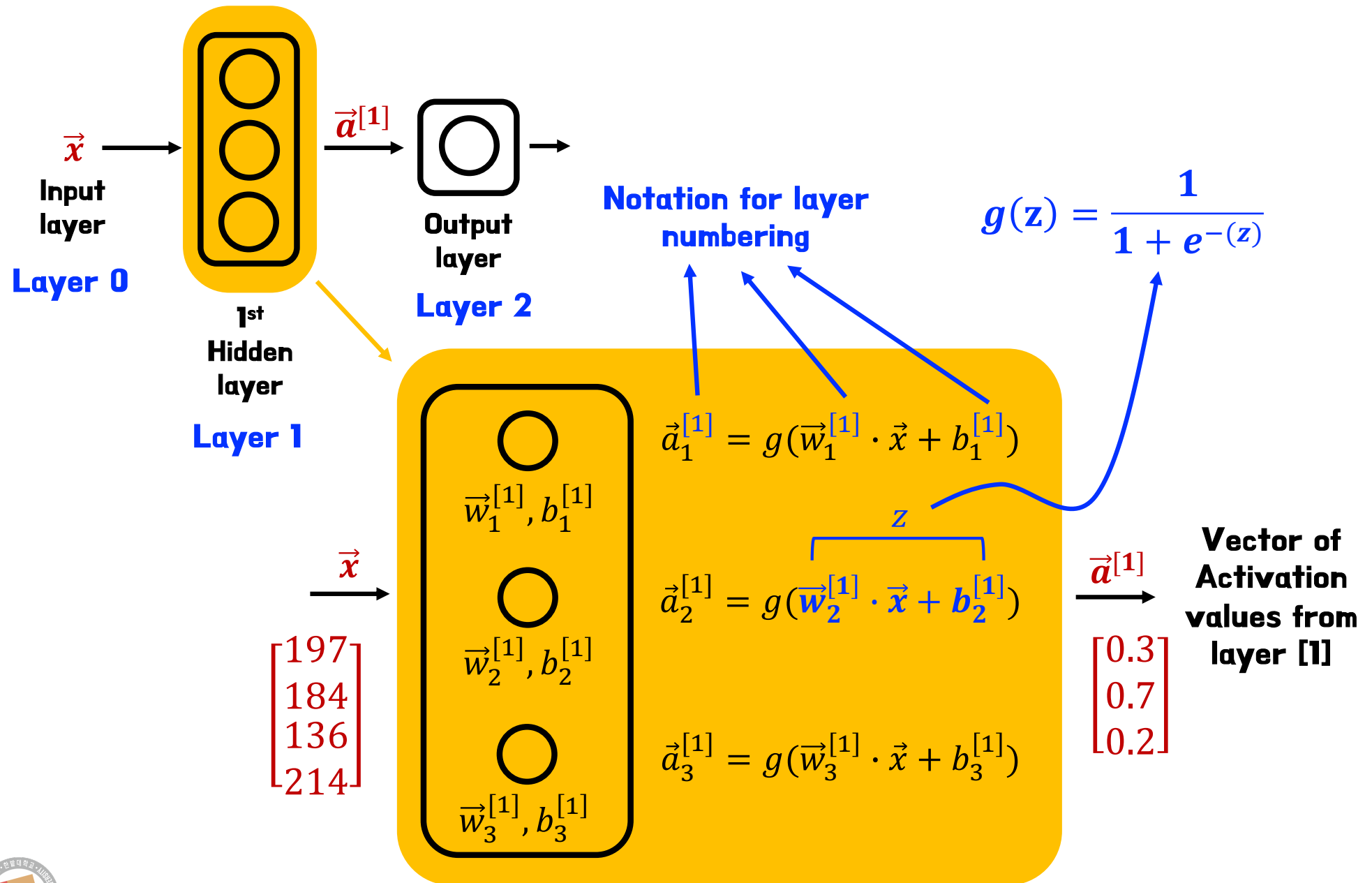
Machine Learning 06

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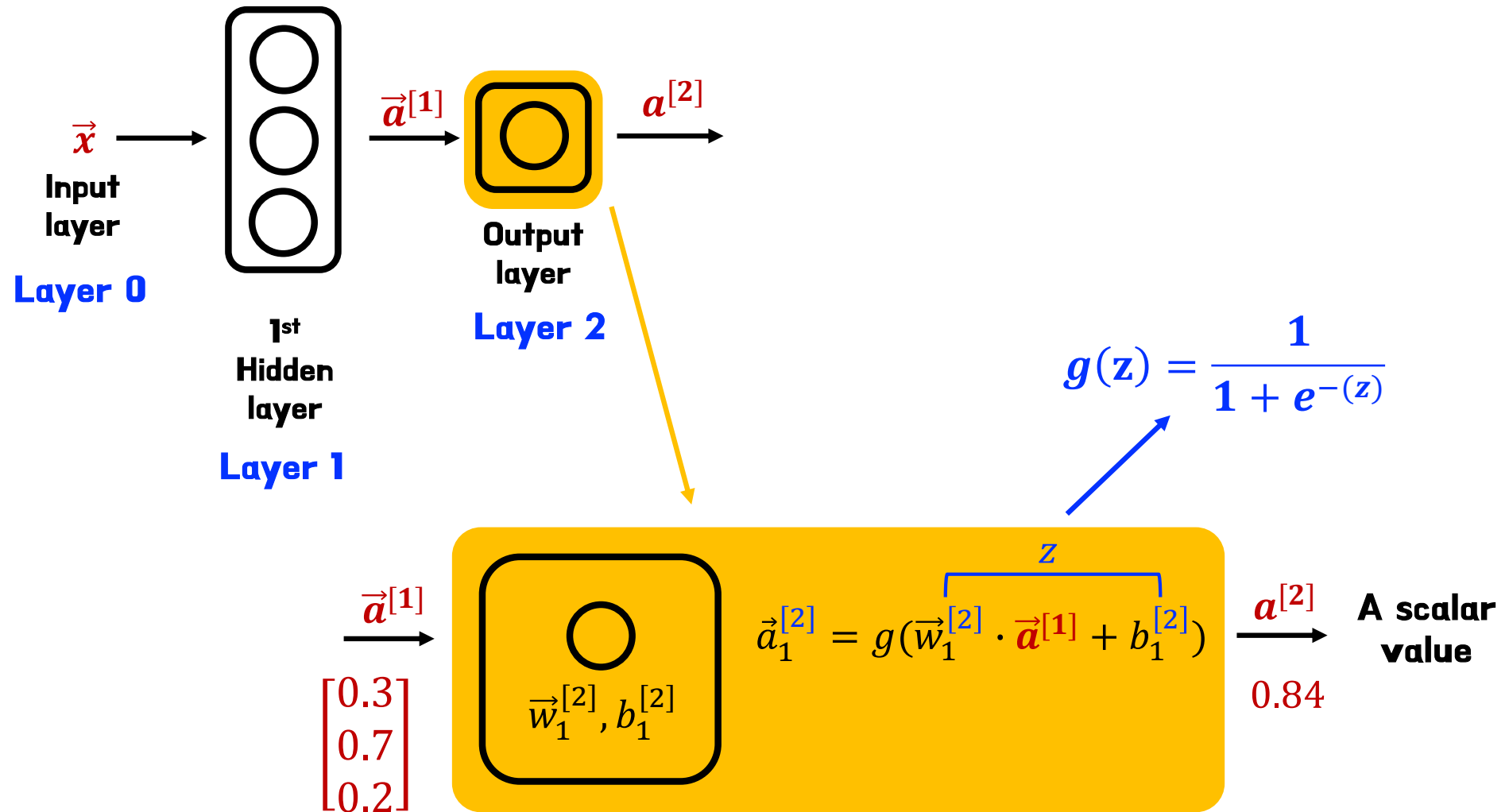
Neural network layer



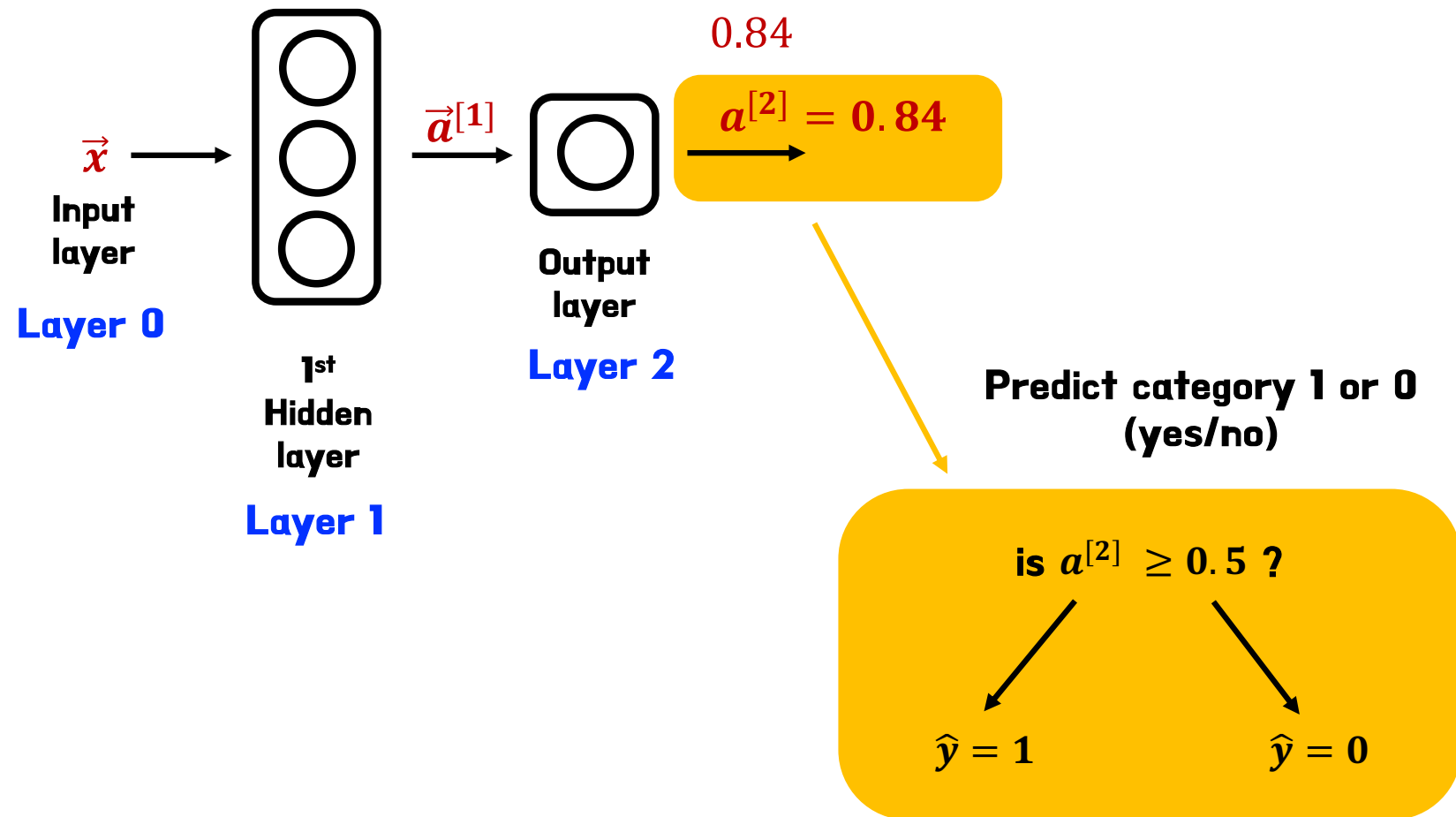
Neural network layer



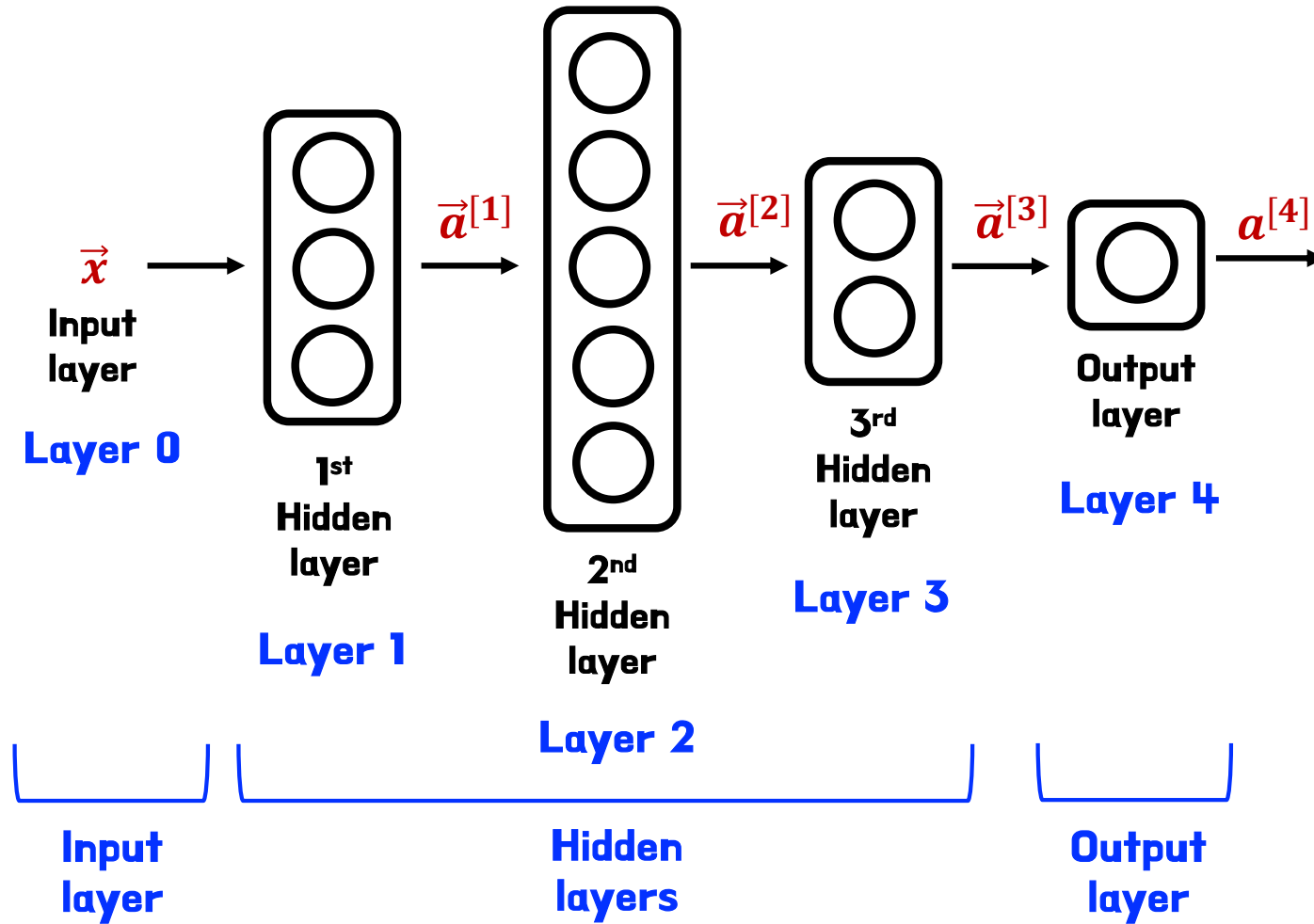
Neural network layer



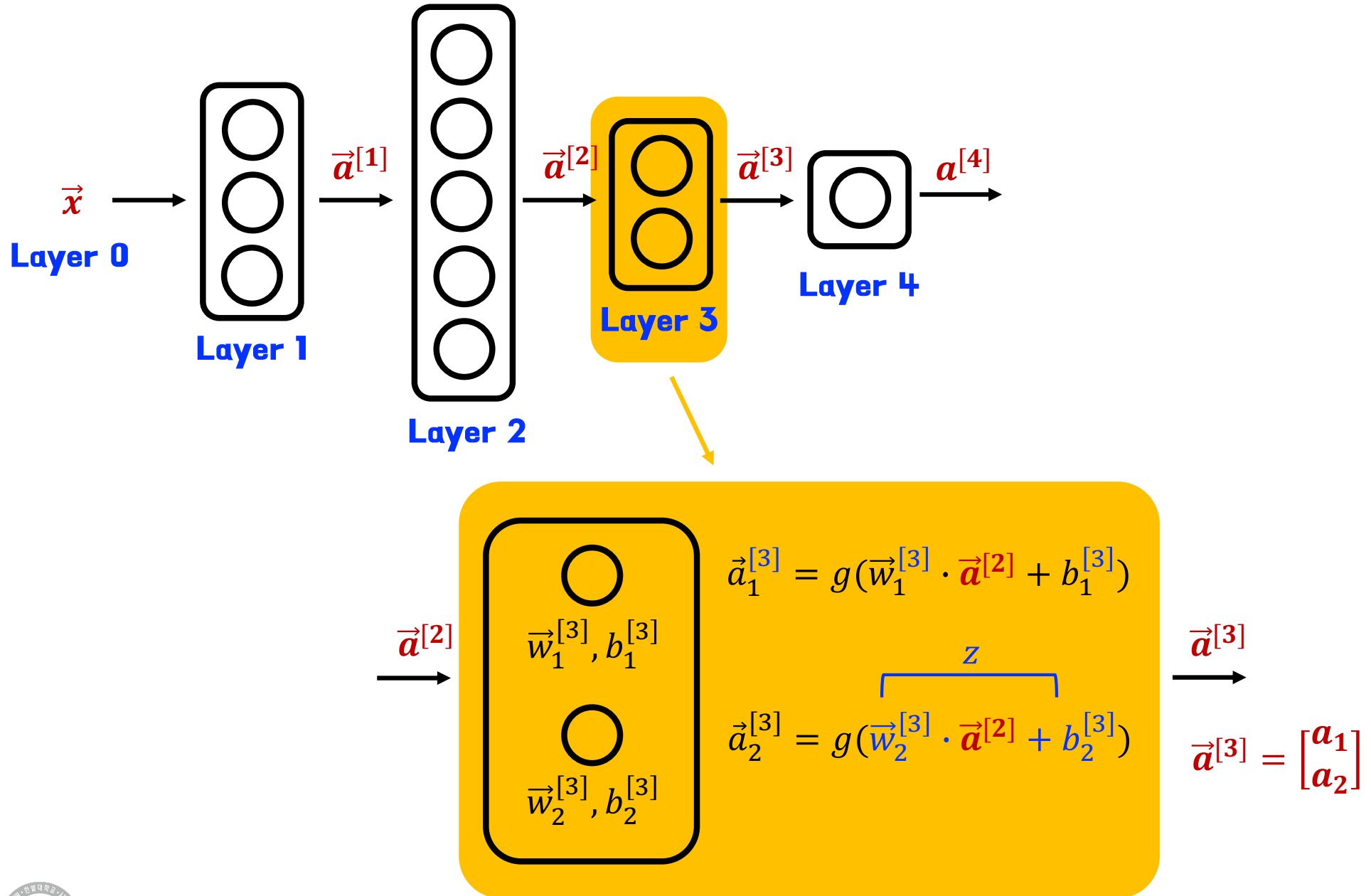
Neural network layer



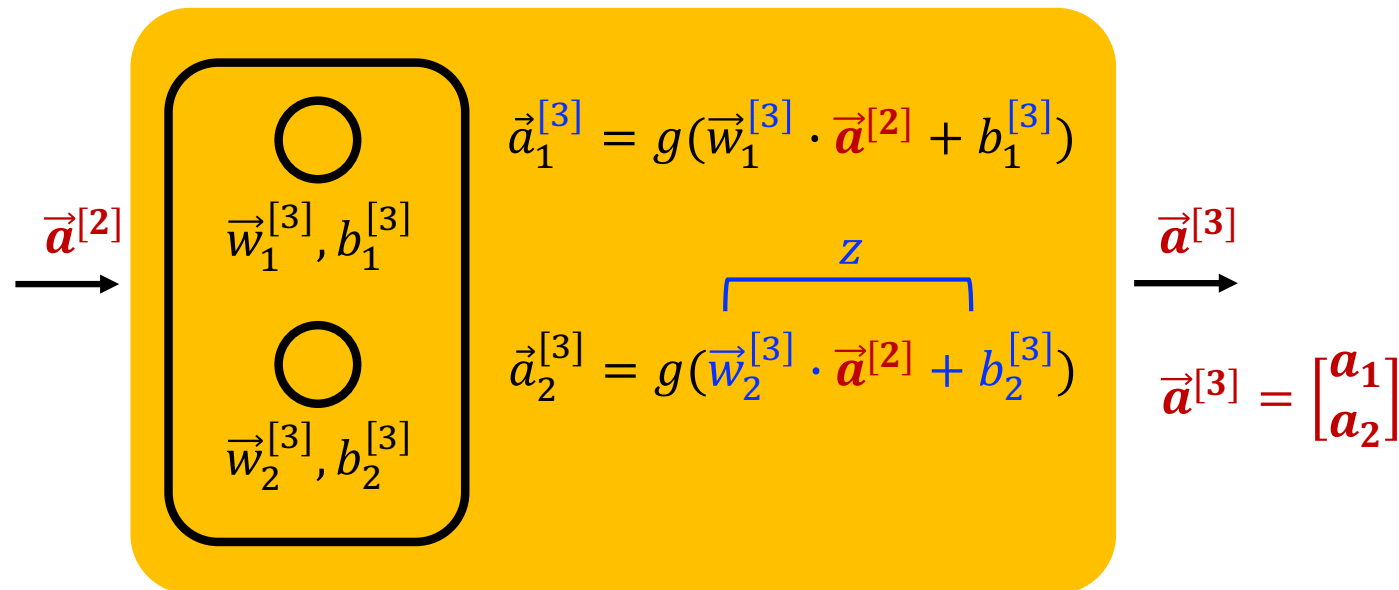
More complex neural network



More complex neural network



More complex neural network



Activation value of layer l , unit (neuron) j

Output of layer $l - 1$ (previous layer)

$$\vec{a}_j^{[l]} = g(\vec{w}_j^{[l]} \cdot \vec{a}^{[l-1]} + b_j^{[l]})$$

Sigmoid "activation function"

Parameters w & b of layer l , unit j



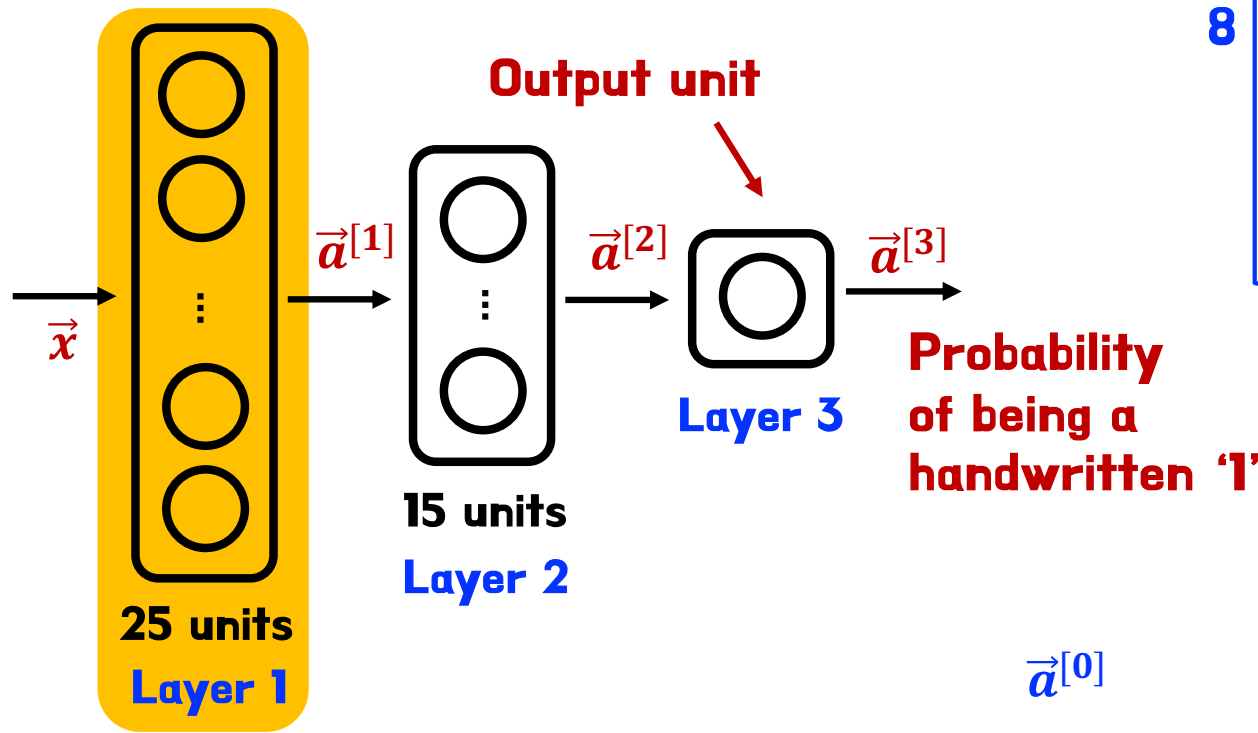
Inference: making predictions (forward propagation)



Handwritten digit recognition

Digit images **0** **1**
 Label **0** **1**

255	255	255	255	255	255	255	255
255	255	255	0	255	255	255	255
255	255	0	0	255	255	255	255
255	255	255	0	255	255	255	255
255	255	255	0	255	255	255	255
255	255	255	0	255	255	255	255
255	255	0	0	0	255	255	255
255	255	255	255	255	255	255	255



**Hidden units
(neurons)**

$$\vec{a}^{[1]} = \begin{bmatrix} g(\vec{w}_1^{[1]} \cdot \vec{x} + b_1^{[1]}) \\ \dots \\ g(\vec{w}_{25}^{[1]} \cdot \vec{x} + b_{25}^{[1]}) \end{bmatrix}$$



Handwritten digit recognition

Digit images



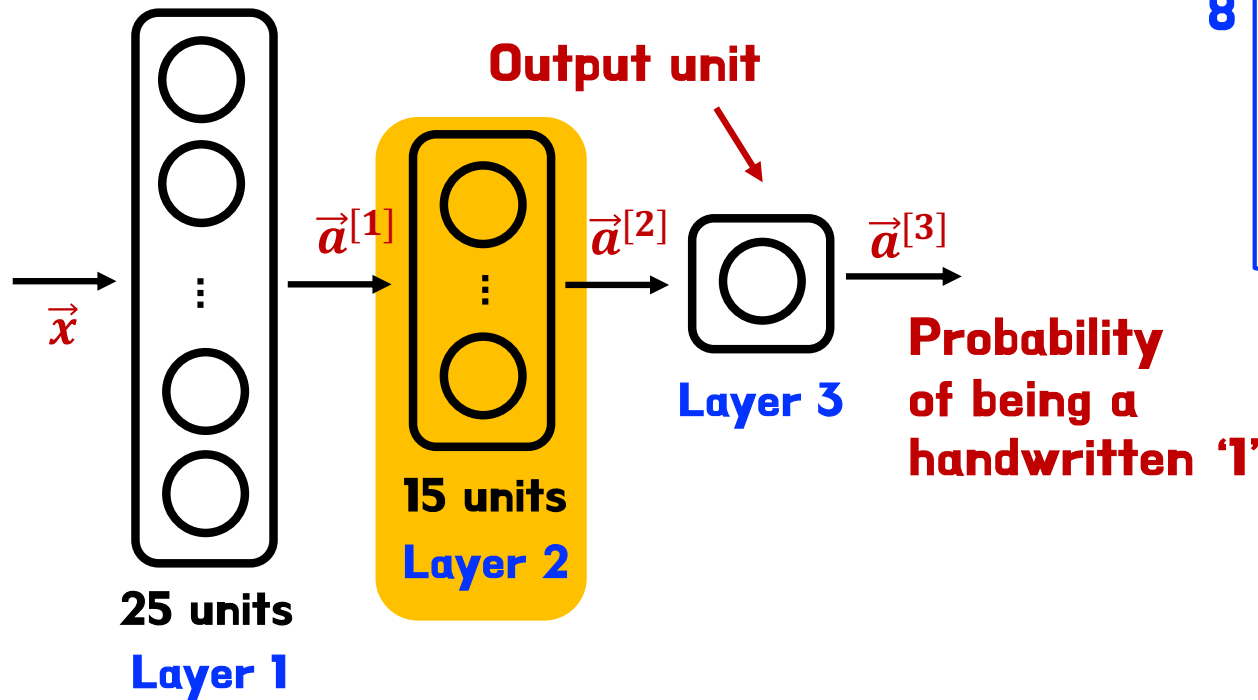
Label



8

255	255	255	255	255	255	255	255
255	255	255	0	255	255	255	255
255	255	0	0	255	255	255	255
255	255	255	0	255	255	255	255
255	255	255	0	255	255	255	255
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255	255	0	0	0	255	255	255
255	255	255	255	255	255	255	255

8



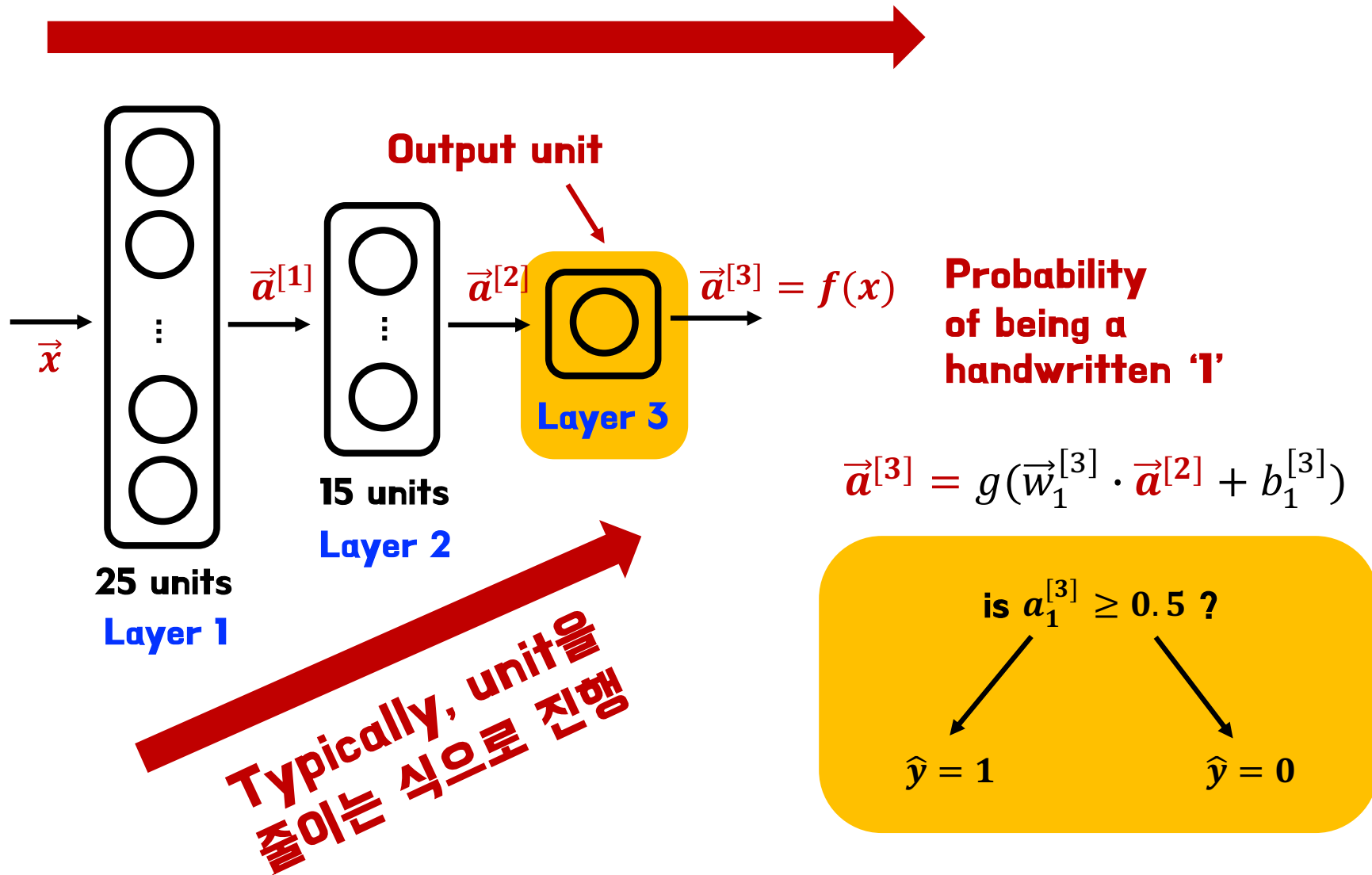
Hidden units (neurons)

$$\vec{a}^{[2]} = \begin{bmatrix} g(\vec{w}_1^{[2]} \cdot \vec{a}^{[1]} + b_1^{[2]}) \\ \dots \\ g(\vec{w}_{15}^{[2]} \cdot \vec{a}^{[1]} + b_{15}^{[2]}) \end{bmatrix}$$



Handwritten digit recognition

Forward propagation



Speculation on artificial general intelligence (AGI)



AI



ANI

**(artificial
narrow
intelligence)**

**e.g.) smart speaker,
self-driving car, web
search, AI in farming
and factories**

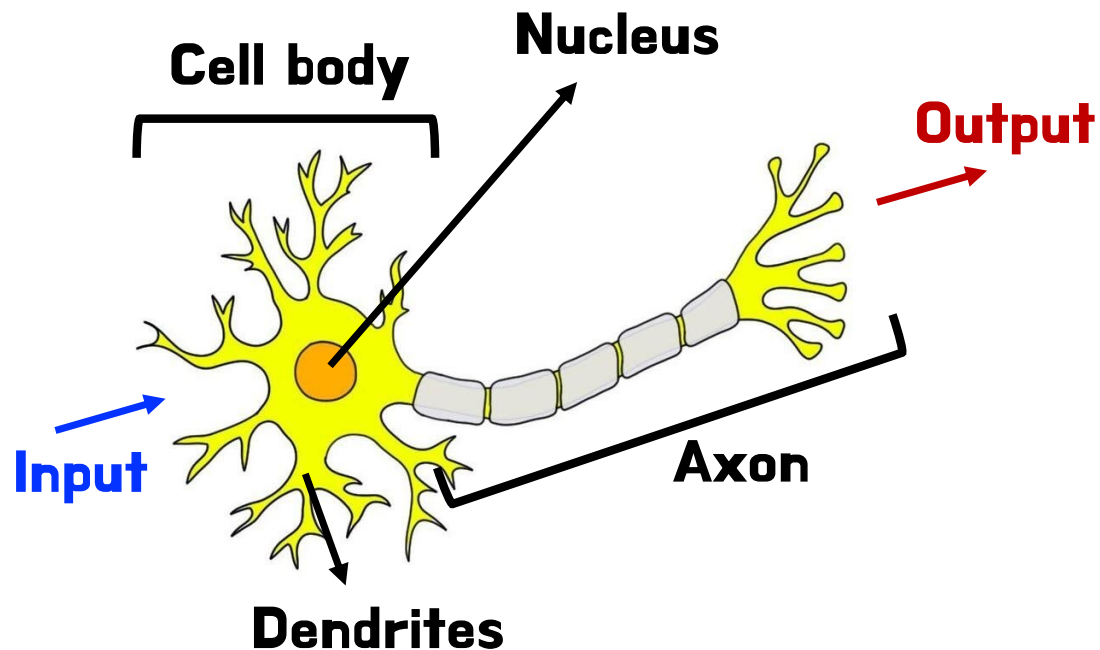
AGI

**(artificial
narrow
intelligence)**

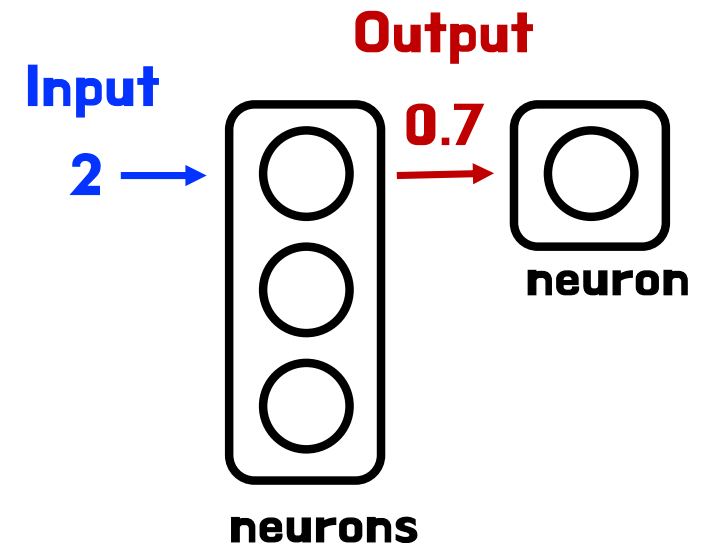
**Do anything a
human can do**

Neural network and the brain

Biological neuron



Simplified mathematical model of a neuron

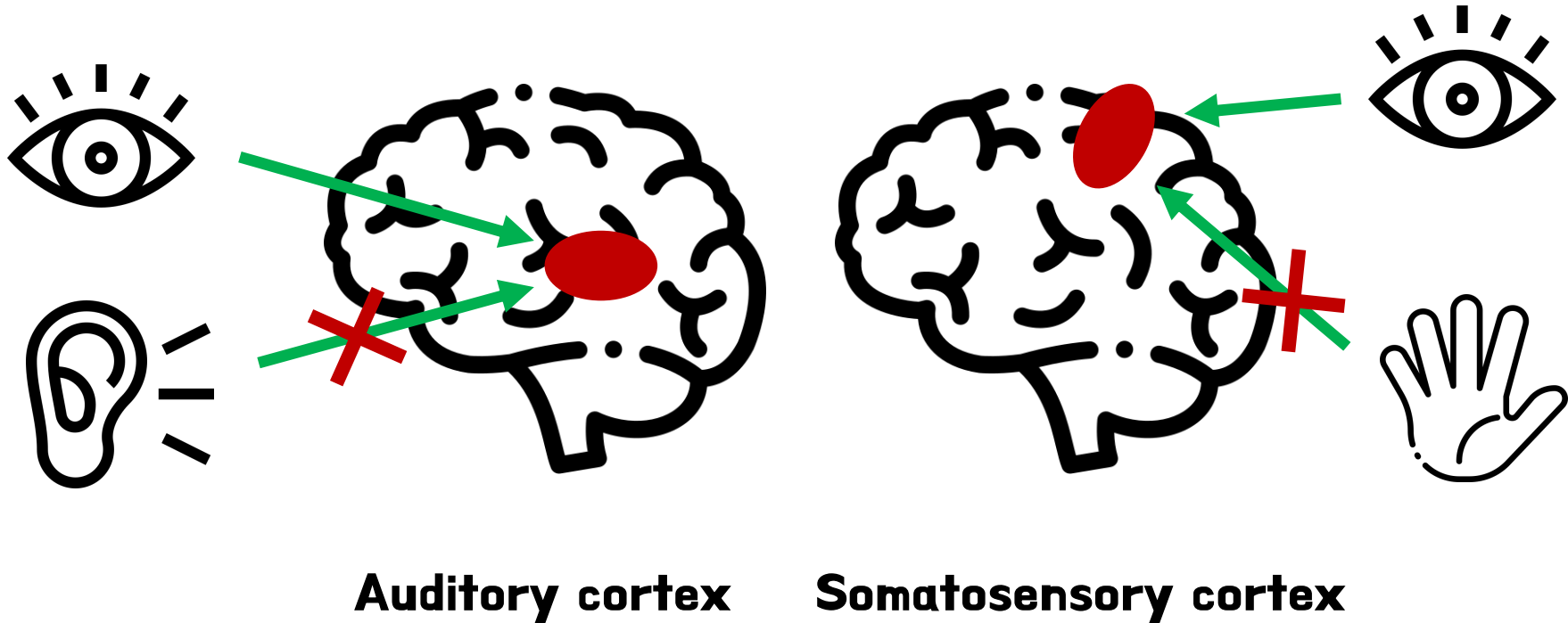


Can we mimic the human brain ?

1. Machine learning is too simple
2. We don't know how the brain works



The “one learning algorithm” hypothesis



One brain cortex can learn other sense as well

Sensor representations in the brain

We don't know if it is possible in machine learning



Seeing with your tongue



Human echolocation (sonar)



Haptic belt: Direction sense

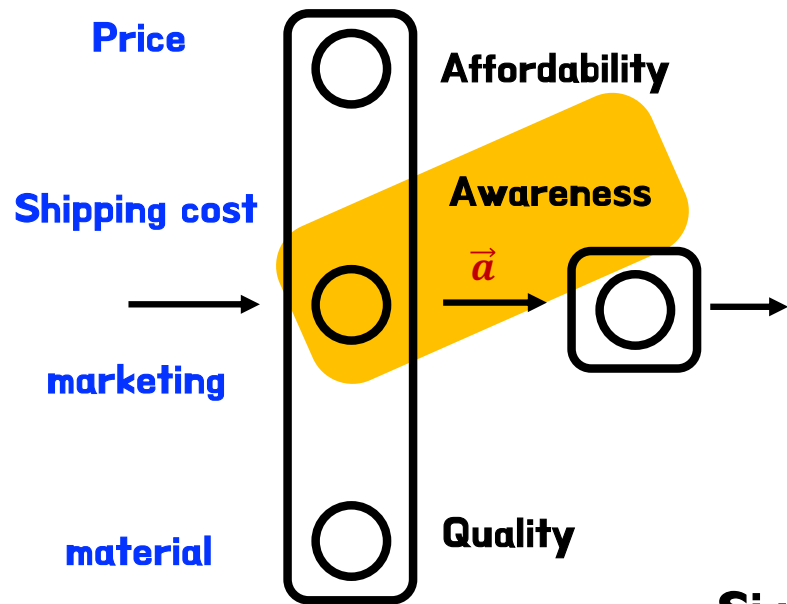


Implanting a 3rd eye

Activation function

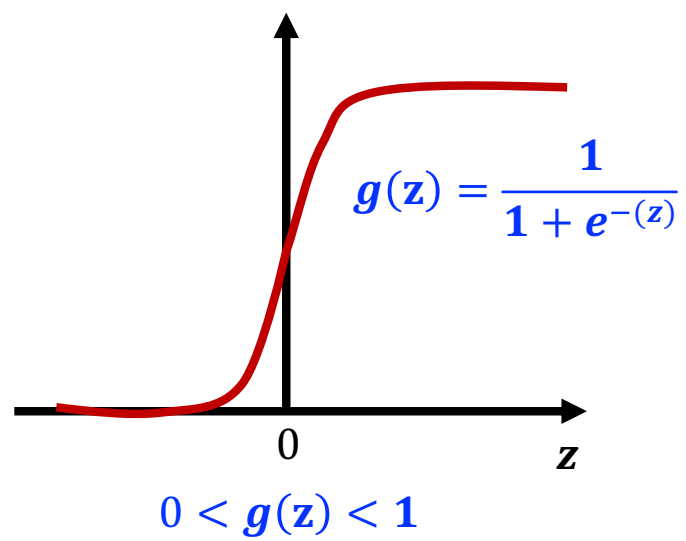


Demand prediction example

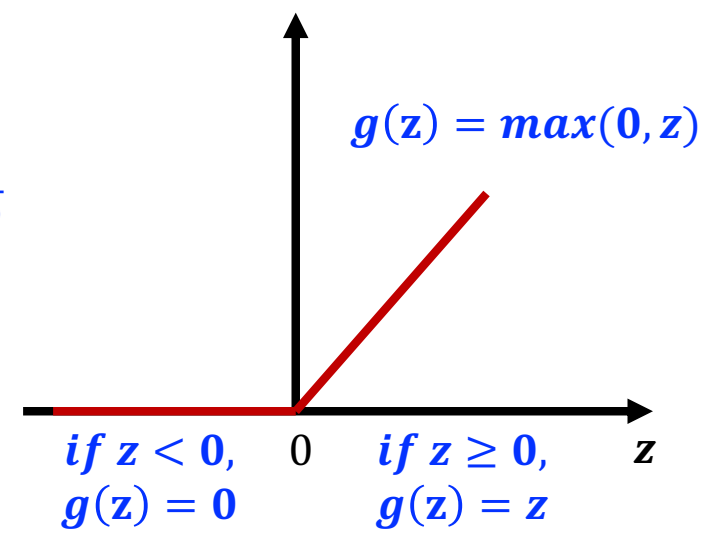


$$a_2^{[1]} = g(\vec{w}_2^{[1]} \cdot \vec{x} + b_2^{[1]})$$

Sigmoid



**ReLU
(Rectified Linear Unit)**

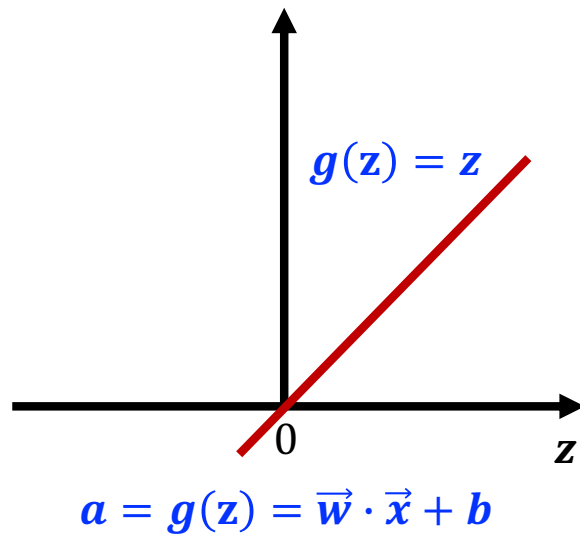


Examples of activation functions

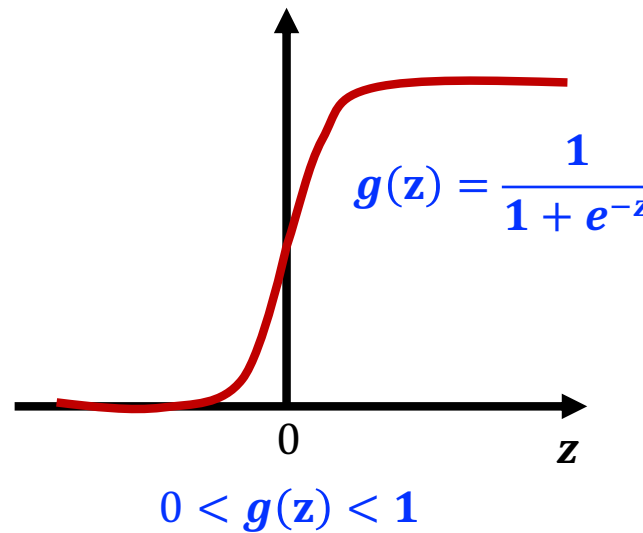
$$a_2^{[1]} = g(\vec{w}_2^{[1]} \cdot \vec{x} + b_2^{[1]})$$

“No activation function”

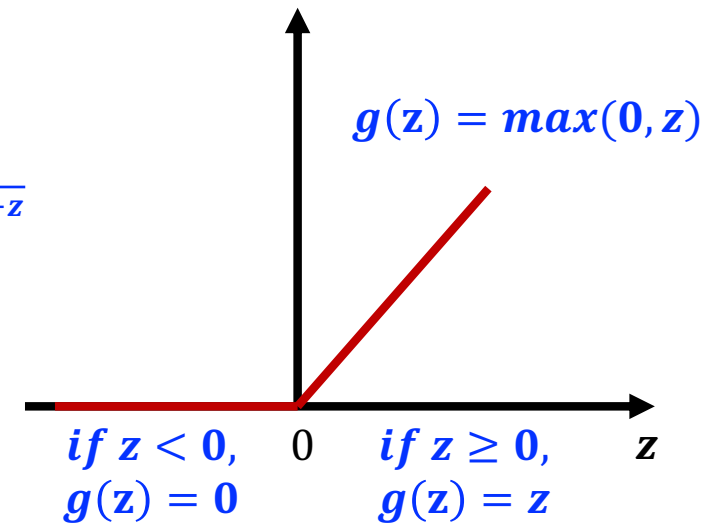
Linear activation
function



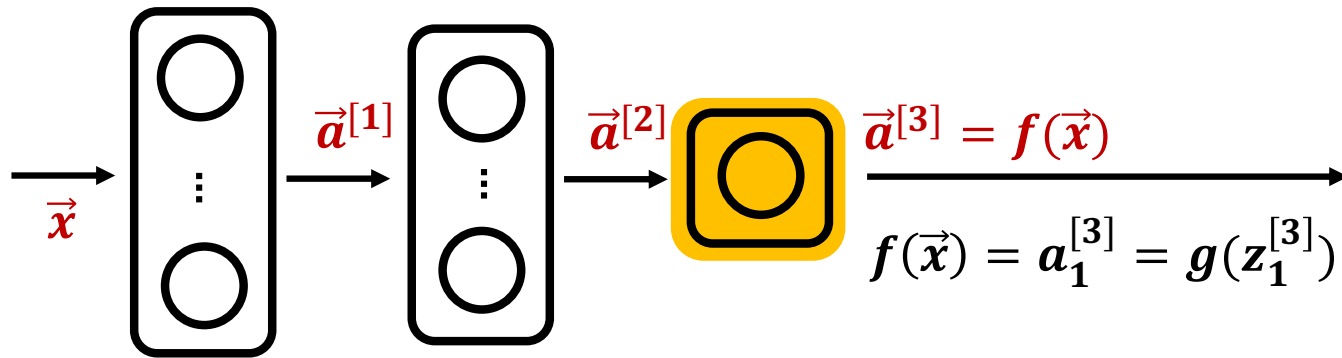
Sigmoid



ReLU
(Rectified Linear Unit)



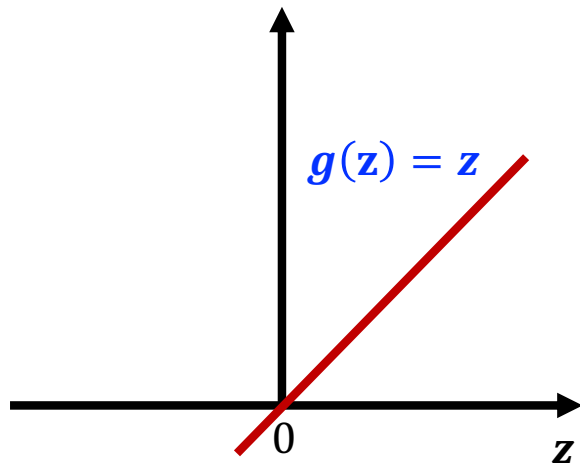
Output layer



Choosing $g(z)$ for output layer ?

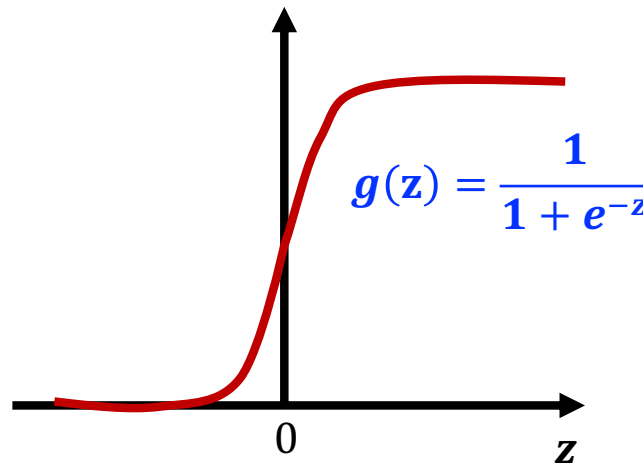
Regression

Linear activation function
 $y = +/-$



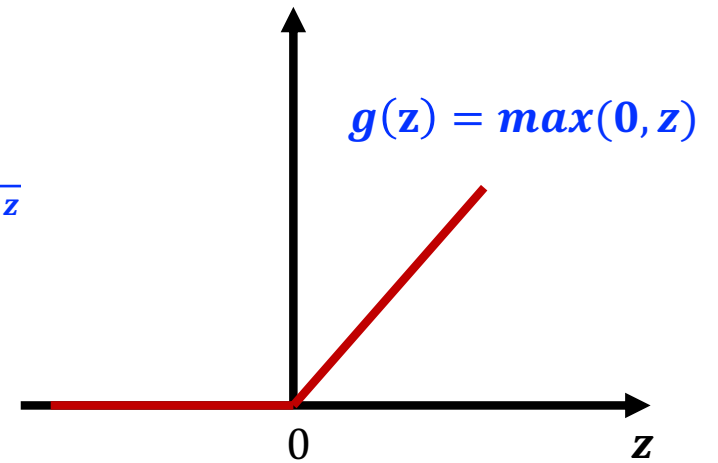
Binary classification

Sigmoid
 $y = 0/1$

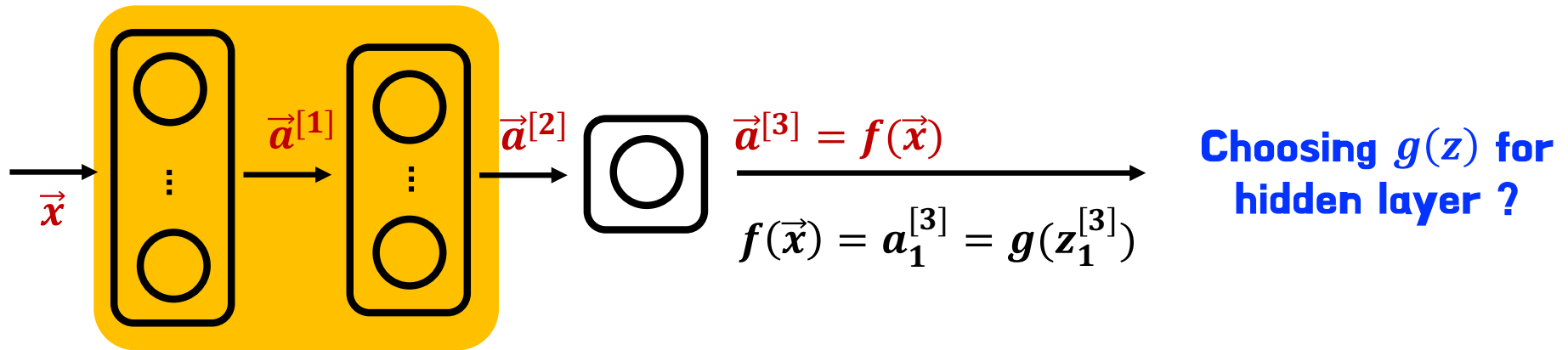


Regression

ReLU
 $y = 0$ or $+$

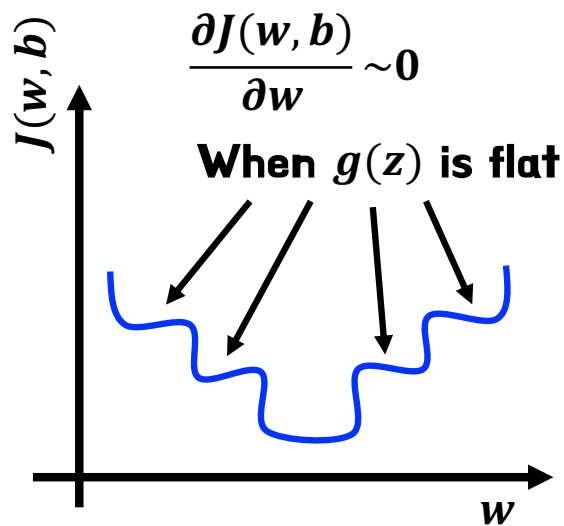
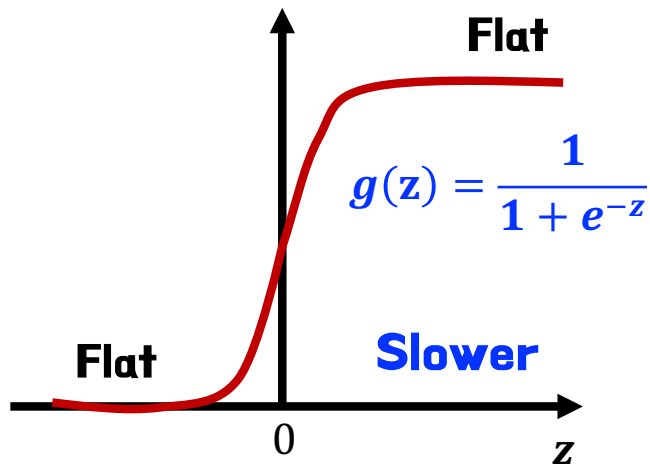


Hidden layer



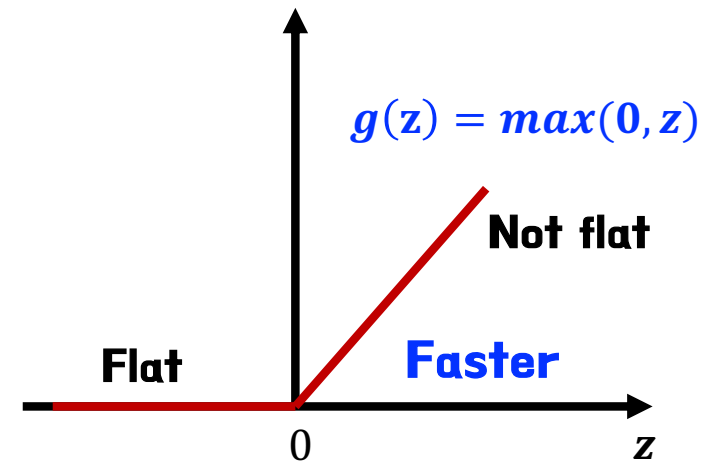
Classical

Sigmoid

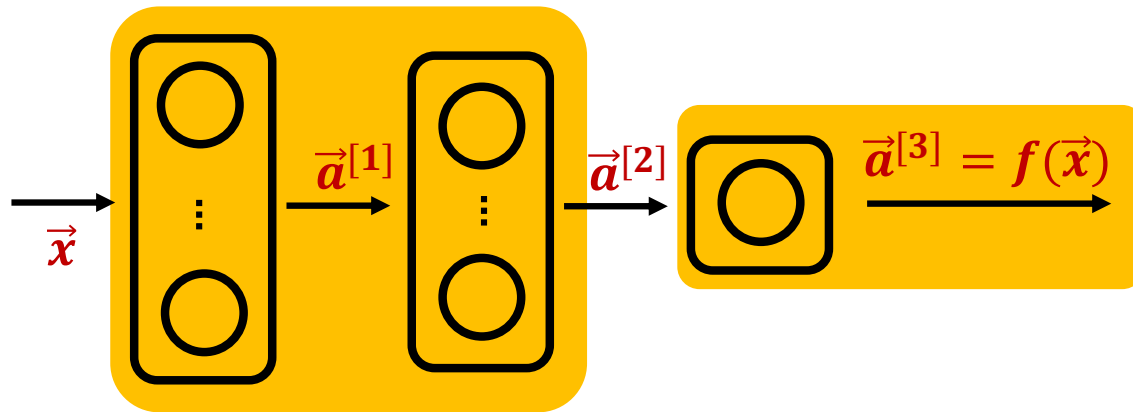


Most common

ReLU



Choosing activation summary



ReLU for hidden layers

Typical coding

```
from tf.keras.layers import Dense
model = Sequential([
    Dense(units=25, activation='relu'),
    Dense(units=15, activation='relu'),
    Dense(units=1, activation='sigmoid'),
])
```

layer1

layer2

layer3 = output layer

Binary classification
Activation = 'sigmoid'

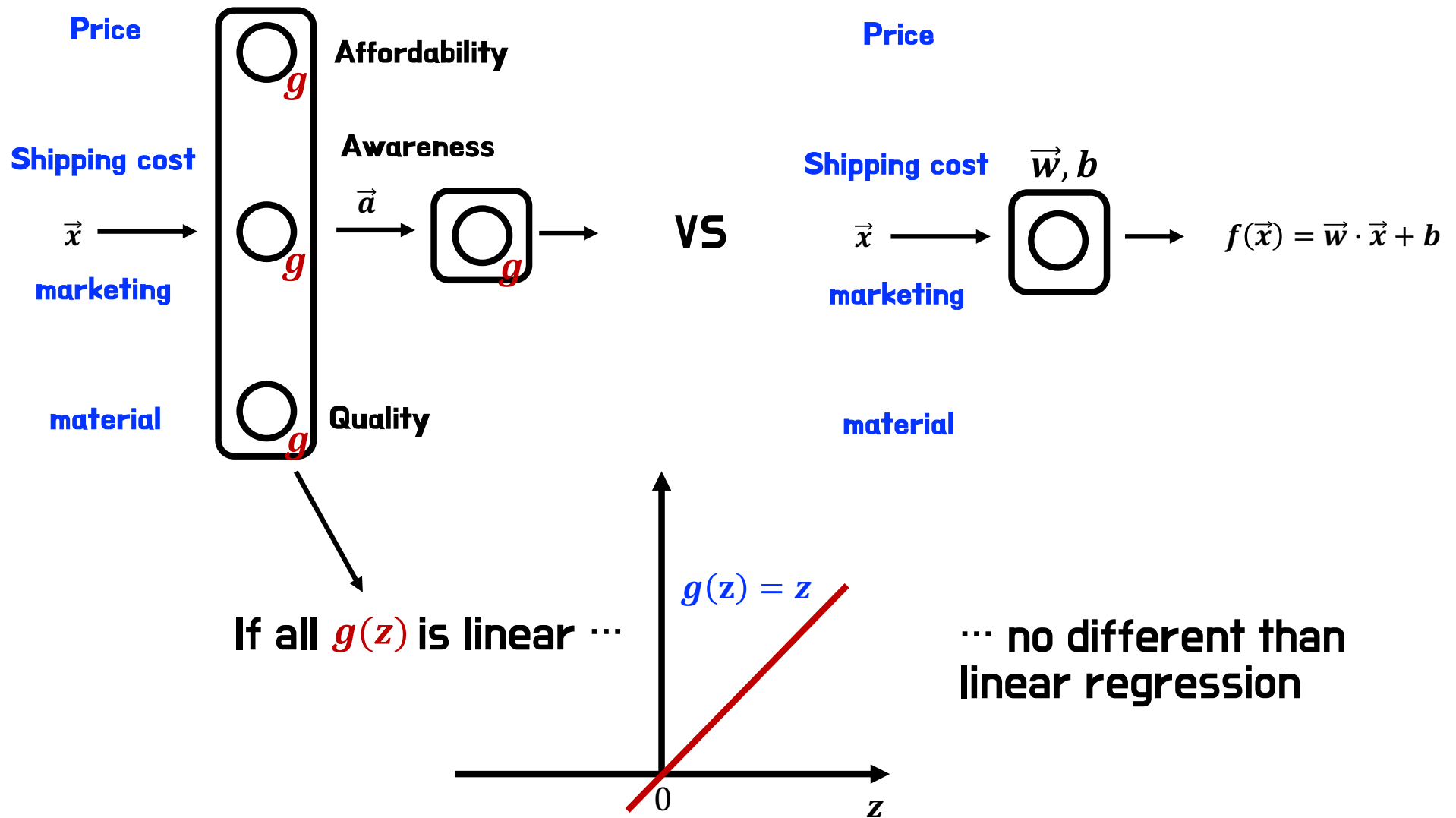
Regression (y: -/+)
Activation = 'linear'

Regression (y: 0/+)
Activation = 'relu'

There are another activation functions: 'Reacky ReLU', 'Tanh', 'Softmax'



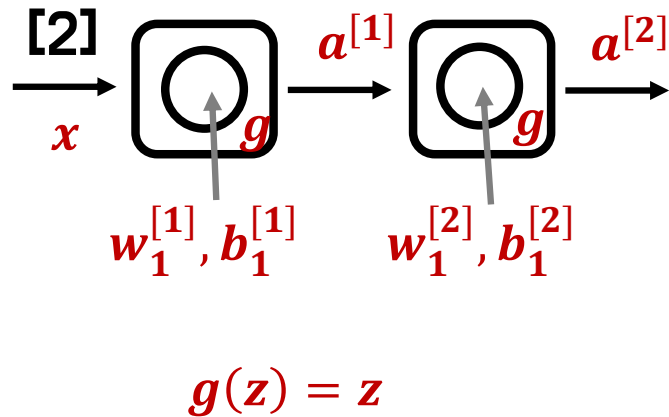
Why do we need activation functions ?



We can't solve complicated cases



Linear example



$$a^{[1]} = w_1^{[1]}x + b_1^{[1]}$$

$$a^{[2]} = w_1^{[2]}a^{[1]} + b_1^{[2]}$$

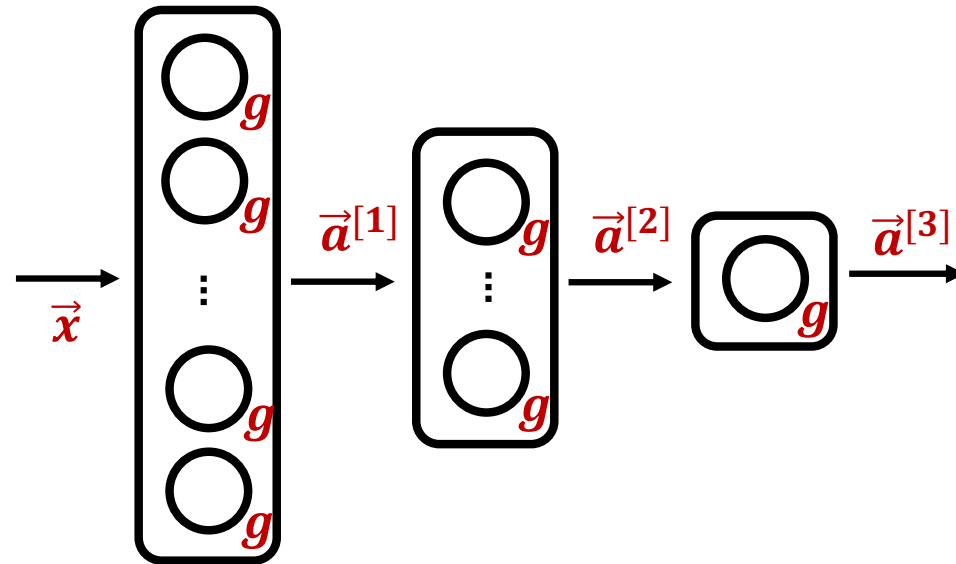
$$= w_1^{[2]}(w_1^{[1]}x + b_1^{[1]}) + b_1^{[2]}$$

$$= \underbrace{w_1^{[2]}w_1^{[1]}}_w x + \underbrace{(w_1^{[2]}b_1^{[1]} + b_1^{[2]})}_b$$

$$a^{[2]} = wx + b$$

Again, same linear regression

Example



$$g(z) = z$$

$$\vec{a}^{[3]} = \vec{w}_1^{[3]} \cdot \vec{a}^{[2]} + b_1^{[3]}$$

All linear (including output)
→ Equivalent to linear regression

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$\vec{a}^{[3]} = \frac{1}{1 + e^{-(\vec{w}_1^{[3]} \cdot \vec{a}^{[2]} + b_1^{[3]})}}$$

Output : sigmoid (hidden : all linear)
→ Equivalent to logistic regression

Don't use linear activation in hidden layers (use ReLU)